Speed Reducers for Precision Motion Control

HarmonicDrive®
Reducer Catalog

- Differential Gear FBB
- Engineering Data

NOTE: This is a section from our full Reducer Product Catalog. Page numbers are for reference only.
Excellent Technology for Evolving Industries

Harmonic Drive® actuators utilize high-precision, zero-backlash Harmonic Drive® precision gears and play critical roles in robotics, semiconductor manufacturing equipment, factory automation equipment, medical diagnostics and surgical robotics. Additionally, our products are frequently used in mission-critical spaceflight applications which capture the human spirit.

With over 50 years of experience, our expert engineering and production teams continually develop enabling technologies for the evolving motion control market. We are proud of our outstanding engineering capabilities and successful history of providing customer specific solutions to meet their application requirements.

Harmonic Drive LLC continues to develop enabling technologies for the evolving motion control market, which drives the pace of global innovation.
Operating Principle of HarmonicDrive® Gears

A simple three-element construction combined with the unique operating principle puts extremely high reduction ratio capabilities into a very compact and lightweight package. The high-performance attributes of this gearing technology including, zero-backlash, high-torque-to-weight ratio, compact size, and excellent positional accuracy, are a direct result of the unique operating principles.

Wave Generator
The Wave Generator is a thin, raced-ball bearing fitted onto an elliptical hub. This serves as a high-efficiency torque converter and is generally mounted onto the input or motor shaft.

Flexspline
The Flexspline is a non-rigid, thin cylindrical cup with external teeth on the open end of the cup. The Flexspline fits over the Wave Generator and takes on its elliptical shape. The Flexspline is generally used as the output of the gear.

Circular Spline
The Circular Spline is a rigid ring with internal teeth. It engages the teeth of the Flexspline across the major axis of the Wave Generator ellipse. The Circular Spline has two more teeth than the Flexspline and is generally mounted onto a housing.

The Flexspline is slightly smaller in diameter than the Circular Spline and usually has two fewer teeth than the Circular Spline. The elliptical shape of the Wave Generator causes the teeth of the Flexspline to engage the Circular Spline at two opposite regions across the major axis of the ellipse.

As the Wave Generator rotates the teeth of the Flexspline engage with the Circular Spline at the major axis.

For every 180 degree clockwise movement of the Wave Generator, the Flexspline rotates counterclockwise by one tooth in relation to the Circular Spline.

Each complete clockwise rotation of the Wave Generator results in the Flexspline moving counterclockwise by two teeth from its original position, relative to the Circular Spline. Normally, this motion is taken out as output.

Development of HarmonicDrive® Speed Reducers

Harmonic Drive® gears have been evolving since the strain wave gear was first patented in 1955. Our innovative development and engineering teams have led us to significant advances in our gear technology. In 1988, Harmonic Drive successfully designed and manufactured a new tooth profile, the “S” tooth. Since implementing the “S” tooth profile, improvement in life, strength and torsional stiffness have been realized. In the 1990s, we focused engineering efforts on designing gears featuring space savings, higher speed, higher load capacity and higher reliability. Then in the 2000s, significant reduction in size and thickness were achieved, all while maintaining high precision specifications.
Differential Gear FD

Precautions on assembly

It is extremely important to assemble the gear accurately, in proper sequence. Perform assembly based on the following precautions.

1. Avoid assembling with excessive force on Wave Generator bearing. Insert Wave Generator as you rotate it.
2. If the Wave Generator does not have an Oldham coupling, special consideration must be given to ensure that concentricity and inclination are within the specified limits.

The surface of HarmonicDrive® is not anti-rust treated. Apply anti-rust agent to the surface if required. Contact us if you would like us to provide the surface with anti-rust treatment.

Note to prevent corrosion

1. Be sure flatness and skewness are minimized.
2. Make sure there are no burrs or foreign substances.
3. Make sure there is enough room to have the minimum clearance in the housing.
4. When a bolt is inserted into a bolt hole, make sure that the bolt hole is located properly.
5. Bolts should not be tightened at the same time. Apply half of the recommended torque to tighten bolts, and then tighten bolts at recommended torque. The order of tightening bolts should be done diagonally.

Make sure that Circular Spline and Flexspline mesh properly. Do not damage the Flexspline during assembly.

The standard SHG/SHF has not been treated for preventing corrosion. If needed, apply rust prevention on metal surfaces. As a special order, Harmonic Drive LLC can provide stainless steel components or surface treatments.

1. Be sure flatness and skewness are minimized.
2. Make sure there are no burrs or foreign substances.
3. Make sure there is enough room to have the minimum clearance in the housing.
4. Make sure that the Circular Spline can rotate in the housing when it is installed.
5. When a bolt is inserted into a bolt hole, make sure that the bolt hole is located properly.
6. Bolts should not be tightened at the same time. Apply half of the recommended torque to tighten bolts, and then tighten bolts at the recommended torque. The order of tightening bolts should be done diagonally.

Avoid using pins to secure the Circular Spline if possible.
Features

The FBB was developed as a versatile simple differential drive transmission for direct phasing of rotating elements while they are in motion. Offsetting internal gear ratios deliver a through ratio of 1:1 and trim adjustments can be applied through one or both of two wave generators.

Features

- For dynamic registration of rotating elements
- A 1:1 differential with high-ratio trim adjustment
- Ideal differential for roll registration or angular shaft phasing
- Compact, low-backlash design for end-of-roll mounting

Axially Compact, Single-Stage, High-Ratio Gearing

DYNAMIC CIRCULAR SPLINE:
An internal gear which has the same number of teeth as the Flexspline and which rotates at the same speed and in the same direction as the Flexspline. It usually is the output element to which an output shaft is connected.

FLEXSPLINE:
External spline teeth that progressively engage the internal teeth of the Static Circular Spline and Dynamic Circular Spline at the major axis of its rotating elliptical shape. Speed reduction relative to the Wave Generator is equal to one-half the number of teeth on the Flexspline's outside edge. For example, if the Flexspline has 200 teeth, the reduction ratio will be 100:1.

WAVE GENERATOR:
An elliptical bearing and the rotating input element of the transmission. It is connected to a motor or other input shaft and imparts a rotating elliptical shape to the Flexspline.

STATIC CIRCULAR SPLINE:
A fixed nonrotating internal gear which provides mechanical grounding for the transmission. It has two more teeth than the Flexspline to establish a positive transmission reduction ratio equal to one-half the number of Flexspline teeth.
FBB Phasing Differential Gear Sets

Harmonic Drive FBB gear sets allow easy and direct phasing of rotating elements and are ideally suited for web presses and other machines requiring constant monitoring and adjustment while they are in motion.

**Drive Power**

FBB is essentially two FB pancake gear sets mounted back to back with dynamic splines connected. The FBB provides a 1:1 through ratio from a primary drive source to secondary elements of a machine with optional speed or position adjustment.

Power is applied to S1, the first of three ring gears called circular splines. Torque is transmitted from the first circular spline to the third circular spline S2, through two gear ratios.

The first ratio is a slight speed increase between S1 and the middle circular spline D.

The second ratio is a very slight speed reduction between the D spline and the S2 circular spline.

When the two wave generators W1 and W2 are stationary, the increasing and decreasing ratios offset each other and the S1 and S2 circular splines rotate in the same direction and at the same speed. Power circulates from the S1 input to the S2 output at a 1:1 ratio with an efficiency of approximately 99%.

**Trim**

With one wave generator W1 rotationally fixed, a second wave generator W2 can be rotated to create, a high ratio advance or retardation (depending on direction) of S2 relative to the S1 circular spline.

Output speed or position can be accurately adjusted with the machine in motion. The output speed of S2 while trim is being applied can be calculated with the following equation:

\[
N_{S2} = N_{S1} \pm \left( \frac{N_{W2}}{(R+1)} \right)
\]

Where

- \( N_{S2} \) = speed
- \( N_{S1} \) = speed
- \( R \) = tabulated ratio

It is possible to attach both wave generators to different drive sources.

For example, W2 could be driven by a servomotor for high-speed automated trim and W1 to a hand crank for low speed manual trim.

Sufficient holding torque must be applied to the trim shaft to prevent rotation. This can be calculated from the following equation:

\[
\text{Control Torque} = \frac{\text{System Output Torque (max)}}{\text{Ratio}} \times 0.5
\]

**Ratio**

Standard ratios are as shown in the rating table page 3, however, other ratios are available on a custom basis (consult our engineering department).

**Ratings**

Torque ratings are as the equivalent size FB pancake gear set.

**Relative Trim Direction**

These examples show the displacement of the circular splines S1 and S2 relative to each other when the wave generator is rotated in the direction of the arrow. Actual rotational direction will depend on the direction of the main input drive.
Ordering Code

**FBB - 20-80-2-SP**

<table>
<thead>
<tr>
<th>Series</th>
<th>Size</th>
<th>Ratio *1</th>
<th>Model</th>
</tr>
</thead>
<tbody>
<tr>
<td>FBB</td>
<td>20</td>
<td>- 80 - 100 - 128 - 160</td>
<td>SP = Special specification code</td>
</tr>
<tr>
<td></td>
<td>25</td>
<td>- 80 - 100 - 120 - 160</td>
<td></td>
</tr>
<tr>
<td></td>
<td>32</td>
<td>78 - 100 - 131 - 157</td>
<td></td>
</tr>
<tr>
<td></td>
<td>40</td>
<td>- 80 - 100 - 128 - 160</td>
<td></td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>- 80 - 100 - 120 - 160</td>
<td></td>
</tr>
</tbody>
</table>

*1 The reduction ratio value is based on the following configuration:
Input: wave generator, fixed: circular spline S, output: circular spline D

Assembly

FBB differentials are supplied as component sets only and are not self contained power transmissions. Suitable housings with bearing supports, oil reservoirs and seals must be provided.

**Circular Splines**
Both S1 & S2 circular splines must be supported with a suitable bearing arrangement to maintain specified dimensions and tolerances under all load conditions.

Overhung loads from an external source require a suitable two-bearing or four-point contact bearing support.

Axial restraint in both directions must maintain the gap between each of the three circular splines.

**Flexspline**
Hardened wear washers are provided to prevent axial displacement of the flexspline. These may be discarded if the customer supplied components in the vicinity of the flexspline are a minimum hardness of Rc45.

**Wave Generator**
The wave generator bearings should not be used to support a shaft. Axial restraint in both directions should be provided.
### Rating table

<table>
<thead>
<tr>
<th>Size</th>
<th>Ratio</th>
<th>Maximum Input Speed rpm</th>
<th>Oil</th>
<th>Grease</th>
<th>Maximum Input Torque Nm</th>
<th>Rated Torque @1750 rpm Nm</th>
<th>Maximum Output Torque Nm</th>
<th>No Load Starting Torque Ncm</th>
<th>Input Inertia kgcm²</th>
</tr>
</thead>
<tbody>
<tr>
<td>20</td>
<td>80</td>
<td>6000 3500</td>
<td>28</td>
<td>28</td>
<td>3.2</td>
<td>0.14</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>100</td>
<td></td>
<td>28</td>
<td>34</td>
<td>3.2</td>
<td>0.14</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>120</td>
<td></td>
<td>28</td>
<td>40</td>
<td>3.2</td>
<td>0.14</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>160</td>
<td></td>
<td>28</td>
<td>44</td>
<td>3.2</td>
<td>0.14</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>25</td>
<td>80</td>
<td>5000 3500</td>
<td>46</td>
<td>48</td>
<td>4.2</td>
<td>0.36</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>100</td>
<td></td>
<td>46</td>
<td>68</td>
<td>4.2</td>
<td>0.36</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>120</td>
<td></td>
<td>46</td>
<td>79</td>
<td>4.2</td>
<td>0.36</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>160</td>
<td></td>
<td>46</td>
<td>88</td>
<td>4.2</td>
<td>0.36</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>32</td>
<td>80</td>
<td>4500 3500</td>
<td>92</td>
<td>107</td>
<td>5.7</td>
<td>1.32</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>100</td>
<td></td>
<td>92</td>
<td>136</td>
<td>5.7</td>
<td>1.32</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>120</td>
<td></td>
<td>92</td>
<td>158</td>
<td>5.7</td>
<td>1.32</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>160</td>
<td></td>
<td>92</td>
<td>175</td>
<td>5.7</td>
<td>1.32</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>40</td>
<td>80</td>
<td>4000 3000</td>
<td>193</td>
<td>192</td>
<td>19.1</td>
<td>3.42</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>100</td>
<td></td>
<td>193</td>
<td>271</td>
<td>19.1</td>
<td>3.42</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>120</td>
<td></td>
<td>193</td>
<td>305</td>
<td>19.1</td>
<td>3.42</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>160</td>
<td></td>
<td>193</td>
<td>350</td>
<td>19.1</td>
<td>3.42</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>50</td>
<td>80</td>
<td>3500 2500</td>
<td>359</td>
<td>350</td>
<td>35.3</td>
<td>9.91</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>100</td>
<td></td>
<td>359</td>
<td>475</td>
<td>35.3</td>
<td>9.91</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>120</td>
<td></td>
<td>359</td>
<td>588</td>
<td>35.3</td>
<td>9.91</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>160</td>
<td></td>
<td>359</td>
<td>655</td>
<td>35.3</td>
<td>9.91</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
A. Item 1 Static Circular Spline  **Marked S**
   Item 2 Spacer
   Item 3 Dynamic Circular Spline  **Marked D**
   Item 4 Flexspline
   Item 5 Wave Generator
   Item 6 Wear washer

B. Dimensions marked 1 established interface and installation requirements and must be maintained under all operating conditions

C. Dimensions marked 2 are necessary to locate wear washers item 6 in correct position. See assembly notes.
<table>
<thead>
<tr>
<th>Size Symbol</th>
<th>20</th>
<th>25</th>
<th>32</th>
<th>40</th>
<th>50</th>
</tr>
</thead>
<tbody>
<tr>
<td>ØA</td>
<td>70.0.018</td>
<td>85.0.020</td>
<td>110.0.020</td>
<td>134.0.020</td>
<td>170.0.018</td>
</tr>
<tr>
<td>B</td>
<td>26.5.0.05</td>
<td>34.8.0.25</td>
<td>42.3.6</td>
<td>56.5.0.4</td>
<td>–</td>
</tr>
<tr>
<td>OC</td>
<td>47.0.51</td>
<td>59.0.51</td>
<td>77.0.51</td>
<td>95.0.51</td>
<td>119.0.51</td>
</tr>
<tr>
<td>OD</td>
<td>54.0.51</td>
<td>69.4.0.51</td>
<td>92.1.0.51</td>
<td>111.1.0.51</td>
<td>134.4.0.51</td>
</tr>
<tr>
<td>OD1</td>
<td>54.7.0.51</td>
<td>70.2.0.51</td>
<td>92.9.0.38</td>
<td>92.9.2.28</td>
<td>135.2.2.28</td>
</tr>
<tr>
<td>E</td>
<td>14.0.1</td>
<td>18.0.1</td>
<td>20.9.1</td>
<td>28.0.1</td>
<td>36.0.2</td>
</tr>
<tr>
<td>F</td>
<td>6.0.1</td>
<td>8.0.1</td>
<td>10.0.2</td>
<td>13.0.2</td>
<td>19.0.2</td>
</tr>
<tr>
<td>G</td>
<td>1.9.51</td>
<td>3.27.51</td>
<td>3.95.51</td>
<td>1.95.51</td>
<td>1.4.51</td>
</tr>
<tr>
<td>H</td>
<td>.81.0.15</td>
<td>.81.0.13</td>
<td>.81.0.15</td>
<td>1.57.0.15</td>
<td>1.57.0.15</td>
</tr>
<tr>
<td>H1</td>
<td>.94.0.15</td>
<td>.94.0.13</td>
<td>.94.0.15</td>
<td>1.69.0.15</td>
<td>1.69.0.15</td>
</tr>
<tr>
<td>ØJ</td>
<td>9.0.10</td>
<td>11.0.18</td>
<td>14.0.20</td>
<td>14.0.20</td>
<td>19.0.20</td>
</tr>
<tr>
<td>ØK</td>
<td>16.0.013</td>
<td>19.0.013</td>
<td>25.0.020</td>
<td>25.0.020</td>
<td>35.0.020</td>
</tr>
<tr>
<td>L</td>
<td>17.4.10</td>
<td>20.8.10</td>
<td>27.3.20</td>
<td>27.3.20</td>
<td>38.3.20</td>
</tr>
<tr>
<td>M</td>
<td>10.4.10</td>
<td>12.8.10</td>
<td>16.3.10</td>
<td>16.3.10</td>
<td>21.8.10</td>
</tr>
<tr>
<td>N</td>
<td>3.0.015</td>
<td>4.0.013</td>
<td>5.0.013</td>
<td>5.0.013</td>
<td>6.0.013</td>
</tr>
<tr>
<td>P</td>
<td>3.0.015</td>
<td>4.0.013</td>
<td>5.0.013</td>
<td>5.0.013</td>
<td>10.0.020</td>
</tr>
<tr>
<td>Q</td>
<td>11.4</td>
<td>12.8</td>
<td>15.6</td>
<td>19.4</td>
<td>23.2</td>
</tr>
<tr>
<td>R</td>
<td>M4 x 0.7</td>
<td>M5 x 0.8</td>
<td>M6 x 1</td>
<td>M8 x 1.25</td>
<td>M10 x 1.5</td>
</tr>
<tr>
<td>ØS</td>
<td>60</td>
<td>75</td>
<td>100</td>
<td>120</td>
<td>150</td>
</tr>
<tr>
<td>ØT</td>
<td>20</td>
<td>28</td>
<td>36</td>
<td>32</td>
<td>50</td>
</tr>
<tr>
<td>Y</td>
<td>M4 x 0.7</td>
<td>M4 x 0.7</td>
<td>M6 x 1.0</td>
<td>M8 x 1.25</td>
<td>M8 x 1.25</td>
</tr>
<tr>
<td>ØZ</td>
<td>27</td>
<td>35</td>
<td>44</td>
<td>48</td>
<td>55</td>
</tr>
<tr>
<td>aa</td>
<td>0.07</td>
<td>0.076</td>
<td>0.078</td>
<td>0.088</td>
<td>0.098</td>
</tr>
<tr>
<td>bb</td>
<td>0.013</td>
<td>0.015</td>
<td>0.015</td>
<td>0.018</td>
<td>0.020</td>
</tr>
<tr>
<td>cc</td>
<td>0.016</td>
<td>0.023</td>
<td>0.025</td>
<td>0.025</td>
<td>0.025</td>
</tr>
<tr>
<td>dd</td>
<td>0.010</td>
<td>0.013</td>
<td>0.013</td>
<td>0.013</td>
<td>0.015</td>
</tr>
<tr>
<td>ee</td>
<td>0.250</td>
<td>0.250</td>
<td>0.250</td>
<td>0.250</td>
<td>0.250</td>
</tr>
<tr>
<td>mass (lb/kgf)</td>
<td>1.50/70</td>
<td>2.70/1.23</td>
<td>4.70/2.14</td>
<td>9.00/4.09</td>
<td>15.30/6.9</td>
</tr>
</tbody>
</table>

Units: mm
## Engineering Data

<table>
<thead>
<tr>
<th>Topic</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tooth profile</td>
<td>009</td>
</tr>
<tr>
<td>Rotational direction and reduction ratio</td>
<td>010</td>
</tr>
<tr>
<td>Gearheads &amp; Actuators</td>
<td>010</td>
</tr>
<tr>
<td>Grease lubricant</td>
<td>018</td>
</tr>
<tr>
<td>Oil lubricant</td>
<td>018</td>
</tr>
<tr>
<td>Lubricant for special environments</td>
<td>019</td>
</tr>
<tr>
<td>Torsional stiffness</td>
<td>020</td>
</tr>
<tr>
<td>Positional accuracy</td>
<td>021</td>
</tr>
<tr>
<td>Vibration</td>
<td>021</td>
</tr>
<tr>
<td>Starting torque</td>
<td>022</td>
</tr>
<tr>
<td>Backdriving torque</td>
<td>022</td>
</tr>
<tr>
<td>No-load running torque</td>
<td>023</td>
</tr>
<tr>
<td>Efficiency</td>
<td>023</td>
</tr>
<tr>
<td>Design guidelines</td>
<td>024</td>
</tr>
<tr>
<td>Assembly guidelines</td>
<td>028</td>
</tr>
<tr>
<td>Checking output bearing</td>
<td>030</td>
</tr>
</tbody>
</table>

### Tooth Profile

Harmonic Drive developed a unique gear tooth profile that optimizes the tooth engagement. It has a special curved surface unique to the S tooth profile that allows continuous contact with the tooth profile. It also alleviates the concentration of stress by widening the width of the tooth groove against the tooth thickness and enlarging the radius on the bottom. This tooth profile (the “S tooth”) enables up to 30% of the total number of teeth to be engaged simultaneously. Additionally, the large tooth root radius increases the tooth strength compared with an involute tooth. This technological innovation results in high torque, high torsional stiffness, long life and smooth rotation.

### S Tooth Profile

- **Patented**

---

### Design Guidelines

- Design guideline
- Bearing support of the input and output shafts
- Wave Generator

### Assembly Guidelines

- Sealing
- Assembly Precautions
- "dedoidal" state

### Checking Output Bearing

- Checking procedure
- How to calculate the maximum moment load
- How to calculate the average load
- How to calculate the radial load coefficient (X) and axial load coefficient (Y)
- How to calculate life
- How to calculate the life under oscillating movement
- How to calculate the static safety coefficient
Tooth Profile

■ S tooth profile

Harmonic Drive developed a unique gear tooth profile that optimizes the tooth engagement. It has a special curved surface unique to the S tooth profile that allows continuous contact with the tooth profile. It also alleviates the concentration of stress by widening the width of the tooth groove against the tooth thickness and enlarging the radius on the bottom. This tooth profile (the "S tooth") enables up to 30% of the total number of teeth to be engaged simultaneously.

Additionally the large tooth root radius increases the tooth strength compared with an involute tooth. This technological innovation results in high torque, high torsional stiffness, long life and smooth rotation.

*Patented
Rotational direction and reduction ratio

**Cup Style**
Series: CSG, CSF, CSD, CSF-mini

- **Rotational direction**

  1. **Reducer**
     - Input: Wave Generator (WG)
     - Output: Flexspline (FS)
     - Fixed: Circular Spline (CS)
     - Reduction ratio: \( i = \frac{1}{R} \)

  2. **Reducer**
     - Input: Wave Generator (WG)
     - Output: Circular Spline (CS)
     - Fixed: Flexspline (FS)
     - Reduction ratio: \( i = \frac{R}{R+1} \)

  3. **Reducer**
     - Input: Flexspline (FS)
     - Output: Wave Generator (WG)
     - Fixed: Circular Spline (CS)
     - Reduction ratio: \( i = \frac{R}{R+1} \)

  4. **Overdrive**
     - Input: Circular Spline (CS)
     - Output: Flexspline (FS)
     - Fixed: Wave Generator (WG)
     - Reduction ratio: \( i = \frac{R+1}{R} \)

  5. **Overdrive**
     - Input: Flexspline (FS)
     - Output: Circular Spline (CS)
     - Fixed: Wave Generator (WG)
     - Reduction ratio: \( i = \frac{R}{R+1} \)

  6. **Overdrive**
     - Input: Circular Spline (CS)
     - Output: Flexspline (FS)
     - Fixed: Wave Generator (WG)
     - Reduction ratio: \( i = \frac{R}{R+1} \)

  7. **Differential**
     - When all of the wave generator, the flexspline and the circular spline rotate, Combinations (1) through (6) are available.

**Silk hat**
Series: SHG, SHF, SHD

- **Rotational direction**

  1. **Reducer**
     - Input: Wave Generator (WG)
     - Output: Flexspline (FS)
     - Fixed: Circular Spline (CS)
     - Reduction ratio: \( i = \frac{1}{R} \)

  2. **Reducer**
     - Input: Wave Generator (WG)
     - Output: Circular Spline (CS)
     - Fixed: Flexspline (FS)
     - Reduction ratio: \( i = \frac{R}{R+1} \)

  3. **Reducer**
     - Input: Flexspline (FS)
     - Output: Wave Generator (WG)
     - Fixed: Circular Spline (CS)
     - Reduction ratio: \( i = \frac{R}{R+1} \)

  4. **Overdrive**
     - Input: Circular Spline (CS)
     - Output: Flexspline (FS)
     - Fixed: Wave Generator (WG)
     - Reduction ratio: \( i = \frac{R+1}{R} \)

  5. **Overdrive**
     - Input: Flexspline (FS)
     - Output: Circular Spline (CS)
     - Fixed: Wave Generator (WG)
     - Reduction ratio: \( i = \frac{R}{R+1} \)

  6. **Overdrive**
     - Input: Circular Spline (CS)
     - Output: Flexspline (FS)
     - Fixed: Wave Generator (WG)
     - Reduction ratio: \( i = \frac{R}{R+1} \)

  7. **Differential**
     - When all of the wave generator, the flexspline and the circular spline rotate, Combinations (1) through (6) are available.
Rotational direction

Input Output
(Note) Contact us if you use the product as Accelerator (5) and (6).

1. Reducer
   - Input: Wave Generator
   - Output: Circular Spline D
   - Fixed: Circular Spline S
   - Reduction ratio: \( i = \frac{1}{R} = \frac{Z_f - Z_c}{Z_f} \)

2. Reducer
   - Input: Wave Generator
   - Output: Circular Spline S
   - Fixed: Circular Spline S
   - Reduction ratio: \( i = \frac{1}{R} = \frac{Z_f - Z_c}{Z_f} \)

3. Reducer
   - Input: Circular Spline D
   - Output: Circular Spline S
   - Fixed: Wave Generator
   - Reduction ratio: \( i = \frac{1}{R} = \frac{Z_f - Z_c}{Z_f} \)

4. Overdrive
   - Input: Circular Spline S
   - Output: Circular Spline D
   - Fixed: Wave Generator
   - Ratio: \( R \frac{1}{R} + 1 \)

5. Overdrive
   - Input: Circular Spline S
   - Output: Wave Generator
   - Fixed: Circular Spline D
   - Reduction ratio: \( i = \frac{1}{R} = \frac{Z_f - Z_c}{Z_f} \)

6. Overdrive
   - Input: Circular Spline D
   - Output: Circular Spline S
   - Fixed: Wave Generator
   - Reduction ratio: \( i = \frac{1}{R} = \frac{Z_f - Z_c}{Z_f} \)

7. Differential
   - When all of the Wave Generator, the Circular Spline S and the Circular Spline D rotate, Combinations (1) through (6) are available.

Reduction ratio

The reduction ratio is determined by the number of teeth of the Flexspline and the Circular Spline

\[
\text{Number of teeth of the Flexspline: } Z_f \\
\text{Number of teeth of the Circular Spline: } Z_c
\]

Example

\[
\begin{align*}
\text{Number of teeth of the Flexspline: } & 200 \\
\text{Number of teeth of the Circular Spline: } & 202 \\
\end{align*}
\]

- Input: Wave Generator
  - Output: Circular Spline
  - Fixed: Flexspline
  - Reduction ratio: \( i = \frac{1}{R} = \frac{Z_f - Z_c}{Z_f} \)

- Input: Wave Generator
  - Output: Flexspline
  - Fixed: Circular Spline
  - Reduction ratio: \( i = \frac{1}{R} = \frac{Z_f - Z_c}{Z_f} \)

- Input: Wave Generator
  - Output: Flexspline
  - Fixed: Circular Spline
  - Reduction ratio: \( i = \frac{1}{R} = \frac{Z_f - Z_c}{Z_f} \)

- Input: Wave Generator
  - Output: Flexspline
  - Fixed: Circular Spline
  - Reduction ratio: \( i = \frac{1}{R} = \frac{Z_f - Z_c}{Z_f} \)

- Input: Wave Generator
  - Output: Flexspline
  - Fixed: Circular Spline
  - Reduction ratio: \( i = \frac{1}{R} = \frac{Z_f - Z_c}{Z_f} \)

- Input: Wave Generator
  - Output: Flexspline
  - Fixed: Circular Spline
  - Reduction ratio: \( i = \frac{1}{R} = \frac{Z_f - Z_c}{Z_f} \)

\[ R \] indicates the reduction ratio value from the ratings table.
Rating Table Definitions

See the corresponding pages of each series for values.

■ Rated torque
Rated torque indicates allowable continuous load torque at rated input speed.

■ Limit for Repeated Peak Torque
(see Graph 12-1)
During acceleration and deceleration the Harmonic Drive® gear experiences a peak torque as a result of the moment of inertia of the output load. The table indicates the limit for repeated peak torque.

■ Limit for Average Torque
In cases where load torque and input speed vary, it is necessary to calculate an average value of load torque. The table indicates the limit for average torque. The average torque calculated must not exceed this limit. (calculation formula: Page 14)

■ Limit for Momentary Peak Torque
(see Graph 12-1)
The gear may be subjected to momentary peak torques in the event of a collision or emergency stop. The magnitude and frequency of occurrence of such peak torques must be kept to a minimum and they should, under no circumstance, occur during normal operating cycle. The allowable number of occurrences of the momentary peak torque may be calculated by using formula 13-1.

■ Maximum Average Input Speed
Maximum Input Speed
Do not exceed the allowable rating. (calculation formula of the average input speed: Page 14).

■ Moment of Inertia
The rating indicates the moment of inertia reflected to the gear input.

Life

■ Life of the wave generator
The life of a gear is determined by the life of the wave generator bearing. The life may be calculated by using the input speed and the output load torque.

<table>
<thead>
<tr>
<th>Series name</th>
<th>CSF, CSD, SHF, SHD, CSF-mini</th>
<th>CSG, SHG</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ln</td>
<td>7,000 hours</td>
<td>10,000 hours</td>
</tr>
<tr>
<td>Lai (average life)</td>
<td>35,000 hours</td>
<td>50,000 hours</td>
</tr>
</tbody>
</table>

Life is based on the input speed and output load torque from the rating table.

Calculation formula for Rated Lifetime

\[
\text{Lh} = \text{Ln} \left( \frac{\text{Tr}}{\text{Tav}} \right) \cdot \left( \frac{\text{Nr}}{\text{Nav}} \right)
\]

Where:

- \( \text{Ln} \): Life of L10 or L50
- \( \text{Tr} \): Rated torque
- \( \text{Nr} \): Rated input speed
- \( \text{Tav} \): Average load torque on the output side (calculation formula: Page 14)
- \( \text{Nav} \): Average input speed (calculation formula: Page 14)
Torque Limits

■ Strength of flexspline
The Flexspline is subjected to repeated deflections, and its strength determines the torque capacity of the Harmonic Drive® gear. The values given for Rated Torque at Rated Speed and for the allowable Repeated Peak Torque are based on an infinite fatigue life for the Flexspline. The torque that occurs during a collision must be below the momentary peak torque (impact torque). The maximum number of occurrences is given by the equation below.

Allowable limit of the bending cycles of the flexspline during rotation of the wave generator while the impact torque is applied: 1.0 x 10⁴ (cycles)

The torque that occurs during a collision must be below the momentary peak torque (impact torque). The maximum number of occurrences is given by the equation below.

Calculation formula

\[ N = \frac{1.0 \times 10^4}{2 \times \frac{n}{60} \times t} \]

- Allowable occurrences
- N occurrences
- Time that impact torque is applied
- t sec
- Rotational speed of the wave generator
- n rpm
- The flexspline bends two times per one revolution of the wave generator.

Caution
If the number of occurrences is exceeded, the Flexspline may experience a fatigue failure.

■ Buckling torque
When a highly excessive torque (16 to 17 times rated torque) is applied to the output with the input stationary, the flexspline may experience plastic deformation. This is defined as buckling torque.

* See the corresponding pages of each series for buckling torque values.

Warning
When the flexspline buckles, early failure of the HarmonicDrive® gear will occur.

■ Ratcheting torque
When excessive torque (8 to 9 times rated torque) is applied while the gear is in motion, the teeth between the Circular Spline and Flexspline may not engage properly. This phenomenon is called ratcheting and the torque at which this occurs is called ratcheting torque. Ratcheting may cause the Flexspline to become non-concentric with the Circular Spline. Operating in this condition may result in shortened life and a Flexspline fatigue failure.

* See the corresponding pages of each series for ratcheting torque values.

Caution
When ratcheting occurs, the teeth may not be correctly engaged and become out of alignment as shown in Figure 013-1. Operating the drive in this condition will cause vibration and damage the flexspline.

Once ratcheting occurs, the teeth wear excessively and the ratcheting torque may be lowered.

Figure 013-1

“Dedoidal” condition.

* See the corresponding pages of each series for ratcheting torque values.
In general, a servo system rarely operates at a continuous load and speed. The input rotational speed, load torque change and comparatively large torque are applied at start and stop. Unexpected impact torque may be applied. These fluctuating load torques should be converted to the average load torque when selecting a model number.

As an accurate cross roller bearing is built in the direct external load support (output flange), the maximum moment load, life of the cross roller bearing and the static safety coefficient should also be checked.

Checking the application motion profile
Review the application motion profile. Check the specifications shown in the figure below.

- **Load torque**
  - $T_1$ (Nm)
- **Time**
  - $t_1$ (sec)
- **Output rotational speed**
  - $n_1$ (rpm)

**Normal operation pattern**
- Starting (acceleration) $T_1$, $t_1$, $n_1$
- Steady operation $T_2$, $t_2$, $n_2$
- Stopping (deceleration) $T_3$, $t_3$, $n_3$
- Dwell $T_4$, $t_4$, $n_4$

**Maximum rotational speed**
- Max. output speed no max
- Max. input rotational speed (Restricted by motors) no max

**Emergency stop torque**
When impact torque is applied $T_s$, $t_s$, $n_s$

**Required life**
$L_{10} = L$ (hours)

Flowchart for selecting a size
Please use the flowchart shown below for selecting a size. Operating conditions must not exceed the performance ratings.

Calculate the average load torque applied on the output side from the application motion profile $T_{av}$ (Nm).

$$T_{av} = \frac{\sum_{i} T_i \times t_i}{\sum_{i} t_i}$$

Make a preliminary model selection with the following conditions.

- **Load torque**
  - $T_{n1}$
- **Time**
  - $t_1$, $t_2$, $t_3$, $t_4$
- **Output rotational speed**
  - $n_1$, $n_2$, $n_3$, $n_4$

Obtain the value of each application motion profile.

**Obtain the value of each application motion profile.**

<table>
<thead>
<tr>
<th>Load torque</th>
<th>$T_i$ (Nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time</td>
<td>$t_i$ (sec)</td>
</tr>
<tr>
<td>Output rotational speed</td>
<td>$n_i$ (rpm)</td>
</tr>
</tbody>
</table>

**Normal operation pattern**

| Starting (acceleration) | $T_1$, $t_1$, $n_1$ |
| Steady operation       | $T_2$, $t_2$, $n_2$ |
| Stopping (deceleration)| $T_3$, $t_3$, $n_3$ |
| Dwell                  | $T_4$, $t_4$, $n_4$ |

**Maximum rotational speed**

- Max. output speed no max
- Max. input rotational speed (Restricted by motors) no max

**Emergency stop torque**
When impact torque is applied $T_s$, $t_s$, $n_s$

**Required life**
$L_{10} = L$ (hours)

Check whether the preliminary model number satisfies the following condition from the rating table.
- $n_i$ av $\leq$ Limit for average speed (rpm)
- $n_i$ max $\leq$ Limit for maximum speed (rpm)

Check whether $T_1$ and $T_3$ are less than the repeated peak torque specification.

Check whether $T_3$ is less than the the momentary peak torque specification.

Calculate the maximum input rotational speed from the max. output rotational speed (no max) and the reduction ratio ($R$: ni max (rpm))

$$n_i = \frac{n_i^{max}}{R}$$

Check whether $T_s$ is equal to or less than the wave generator (see Page 13).

Calculate the lifetime.

$$L_{10} = 7000 \times \left( \frac{T_s}{T_{av}} \right)^{b} \times \left( \frac{n_s}{n_i} \right)^{c} (\text{hours})$$

Check whether the calculated life is equal to or more than the life of the wave generator (see Page 13).

The model number is confirmed.
Example of model number selection

<table>
<thead>
<tr>
<th>Value of each application motion profile</th>
<th>Maximum rotational speed</th>
</tr>
</thead>
<tbody>
<tr>
<td>Load torque (Nm)</td>
<td>Max. output speed no max = 14 rpm</td>
</tr>
<tr>
<td>Time (sec)</td>
<td>Max. input speed ni max = 1800 rpm</td>
</tr>
<tr>
<td>Output speed (rpm)</td>
<td>(Restricted by motors)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Normal operation pattern</th>
<th>Emergency stop torque</th>
</tr>
</thead>
<tbody>
<tr>
<td>Starting (acceleration)</td>
<td>When impact torque is applied</td>
</tr>
<tr>
<td>Steady operation (constant velocity)</td>
<td>Ts = 500 Nm, ts = 0.15 sec, ns = 14 rpm</td>
</tr>
<tr>
<td>Stopping (deceleration)</td>
<td></td>
</tr>
<tr>
<td>Dwell</td>
<td></td>
</tr>
</tbody>
</table>

| T1 = 400 Nm, t1 = 0.3sec, n1 = 7rpm          |                          |
| T2 = 320 Nm, t2 = 3sec, n2 = 14rpm          |                          |
| T3 = 200 Nm, t3 = 0.4sec, n3 = 7rpm         |                          |
| T4 = 0 Nm, t4 = 0.2 sec, n4 = 0 rpm         |                          |

<table>
<thead>
<tr>
<th>Output speed n instantaneous max</th>
<th>Required life</th>
</tr>
</thead>
<tbody>
<tr>
<td>Max. output speed no max = 14 rpm</td>
<td>L10 = 7000 (hours)</td>
</tr>
<tr>
<td>Max. input speed ni max = 1800 rpm</td>
<td></td>
</tr>
</tbody>
</table>

Make a preliminary model selection with the following conditions. Tav = 319 Nm \( \leq \) 620 Nm (Limit for average torque for model number CSF-40-120-2A-GR: See the rating table on Page 39.) Thus, CSF-40-120-2A-GR is tentatively selected.

Calculate the average load torque to the output side based on the application motion profile: Tav (Nm).

\[
Tav = \frac{7 \text{ rpm} \cdot 0.3 \text{ sec} \cdot 400 \text{ Nm}^2 + 14 \text{ rpm} \cdot 3 \text{ sec} \cdot 320 \text{ Nm}^2 + 7 \text{ rpm} \cdot 0.4 \text{ sec} \cdot 200 \text{ Nm}^2}{7 \text{ rpm} \cdot 0.3 \text{ sec} + 14 \text{ rpm} \cdot 3 \text{ sec} + 7 \text{ rpm} \cdot 0.4 \text{ sec}}
\]

Calculate the average output rotational speed: no av (rpm)

\[
no av = \frac{7 \text{ rpm} \cdot 0.3 \text{ sec} + 14 \text{ rpm} \cdot 3 \text{ sec} + 7 \text{ rpm} \cdot 0.4 \text{ sec}}{7 \text{ rpm} \cdot 0.3 \text{ sec} + 14 \text{ rpm} \cdot 3 \text{ sec} + 7 \text{ rpm} \cdot 0.4 \text{ sec}} = 12 \text{ rpm}
\]

Check whether the calculated life is equal to or more than the life of the wave generator (see Page 12).

<table>
<thead>
<tr>
<th>Check whether T1 and T3 are equal to or less than the repeated peak torque specification.</th>
<th>NG</th>
</tr>
</thead>
<tbody>
<tr>
<td>T1 = 400 Nm ( \leq ) 617 Nm (Limit of repeated peak torque of size 40)</td>
<td>NG</td>
</tr>
<tr>
<td>T3 = 200 Nm ( \leq ) 617 Nm (Limit of repeated peak torque of size 40)</td>
<td>NG</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Check whether T5 is equal to or less than the momentary peak torque specification.</th>
<th>OK</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ts = 500 Nm ( \leq ) 1180 Nm (Limit for momentary torque of size 40)</td>
<td>OK</td>
</tr>
</tbody>
</table>

Calculate the allowable number (Ns) rotation during impact torque and confirm \( \leq 1.0 \times 10^4 \)

\[
Ns = \frac{10^4}{2 \cdot 14 \text{ rpm} \cdot 120 \text{ rpm} \cdot 0.15 \text{ sec}} = 1190 \leq 1.0 \times 10^4
\]

The selection of model number CSF-40-120-2A-GR is confirmed from the above calculations.
Lubrication

Component Sets: CSD-2A, CSF-2A, CSFG-2A, FB-2, FB-0, FR-2, SHF-2A, SHG-2A and SHD and SHG/SHF -2SO and -2SH gear units: Gear lubricant and oil lubricant are available for lubricating the component sets and SHD gear unit. It is extremely important to properly grease your component sets and SHD gear unit. Proper lubrication is essential for high performance and reliability. Harmonic Drive® component sets are shipped with a rust- preventative oil. The characteristics of the lubricating grease and oil types approved by Harmonic Drive are not changed by mixing with the preservation oil. It is therefore not necessary to remove the preservation oil completely from the gear components. However, the mating surfaces must be degreased before the assembly.

Gear Units: CSG/CSF 2UH and 2UH-LW; CSD-2UF and -2UH; SHG/SHF-2UH and 2UH- LW; SHG/SHF-2UJ; CSF Supermini, CSF Mini, and CSF-2UP.

Gear lubricant is standard for lubricating the gear units. You do not need to apply grease during assembly as the product is lubricated and shipped.

See Page 19 for using lubricant beyond the temperature range in table 16-2.

* Contact us if you want consistency zero (NLGI No.0) for maintenance reasons.

Grease lubricant

■ Types of lubricant

Harmonic Grease® SK-1A

This grease was developed for Harmonic Drive® gears and features good durability and efficiency.

Harmonic Grease® SK-2

This grease was developed for small sized Harmonic Drive® gears and features smooth rotation of the Wave Generator since high pressure additive is liquefied.

Harmonic Grease® 4B No.2

This has been developed exclusively for the CSF and CSG and features long life and can be used over a wide range of temperature.

(Note)

1. Grease lubrication must have proper sealing, this is essential for 4B No.2. Rotating part: Oil seal with spring is needed. Mating part: O ring or seal adhesive is needed.

2. The grease has the highest deterioration rate in the region where the grease is subjected to the greatest shear (near wave generator). Its viscosity is between JIS No.0 and No.00 depending on the operation.

* The hottest section should not be more than 40° above the ambient temperature.

Note: The three basic components of the gear - the Flex spline, Wave Generator and Circular Spline - are matched and serialized in the factory. Depending on the product they are either greased or prepared with preservation oil. Then the individual components are assembled. If you receive several units, please be careful not to mix the matched components. This can be avoided by verifying that the serial numbers of the assembled gear components are identical.

■ Compatible grease by size

Compatible grease varies depending on the size and reduction ratio. See the following compatibility table. We recommend SK-1A and SK-2 for general use.

Ratios 30:1

<table>
<thead>
<tr>
<th>Size</th>
<th>8</th>
<th>11</th>
<th>14</th>
<th>17</th>
<th>20</th>
<th>25</th>
<th>32</th>
</tr>
</thead>
<tbody>
<tr>
<td>SK-1A</td>
<td>◎</td>
<td>◎</td>
<td>◎</td>
<td>◎</td>
<td>◎</td>
<td>◎</td>
<td>◎</td>
</tr>
<tr>
<td>SK-2</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
</tr>
<tr>
<td>4B No.2</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
</tr>
</tbody>
</table>

Ratios 50:1* and above

<table>
<thead>
<tr>
<th>Size</th>
<th>40</th>
<th>45</th>
<th>50</th>
<th>58</th>
<th>65</th>
<th>80</th>
<th>90</th>
<th>100</th>
</tr>
</thead>
<tbody>
<tr>
<td>SK-1A</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
</tr>
<tr>
<td>SK-2</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
</tr>
<tr>
<td>4B No.2</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
</tr>
</tbody>
</table>

* Oil lubrication is required for component-sets size 50 or larger with a reduction ratio of 50:1.

Grease characteristics

<table>
<thead>
<tr>
<th>Grease</th>
<th>SK-1A</th>
<th>SK-2</th>
<th>4B No.2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Durability</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
</tr>
<tr>
<td>Fretting resistance</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
</tr>
<tr>
<td>Low-temperature performance</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
</tr>
<tr>
<td>Grease leakage</td>
<td>☐</td>
<td>☐</td>
<td>☐</td>
</tr>
</tbody>
</table>

* Oil lubrication is required for component-sets size 50 or larger with a reduction ratio of 50:1.

** Note:** Standard grease: ☐ Semi-standard grease: ☐ Recommended grease for long life and high load: ☐ Use Caution: ☐

---

<table>
<thead>
<tr>
<th>Table</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Table 016-1</td>
<td>Name of lubricant</td>
</tr>
<tr>
<td>Table 016-2</td>
<td>Temperature</td>
</tr>
<tr>
<td>Table 016-3</td>
<td>NLGI consistency No. Mixing consistency range</td>
</tr>
<tr>
<td>Table 016-4</td>
<td>Grease specification</td>
</tr>
<tr>
<td>Table 016-5</td>
<td>Ratios 30:1</td>
</tr>
<tr>
<td>Table 016-6</td>
<td>Ratios 50:1* and above</td>
</tr>
<tr>
<td>Table 016-7</td>
<td>Grease characteristics</td>
</tr>
</tbody>
</table>
When to replace grease

The wear characteristics of the gear are strongly influenced by the condition of the grease lubrication. The condition of the grease is affected by the ambient temperature. The graph 017-1 shows the maximum number of input rotations for various temperatures. This graph applies to applications where the average load torque does not exceed the rated torque.

Note: Recommended Grease: SK-1A or SK-2

When to replace grease: $L_{OT}$ (when the average load torque is equal to or less than the rated torque)

$$L_{OT} = L_{OTn} \times \left( \frac{Tr}{Tav} \right)^3$$

Other precautions

1. Avoid mixing different kinds of grease. The gear should be in an individual case when installed.

2. Please contact us when you use HarmonicDrive® gears at constant load or in one direction continuously, as it may cause lubrication problems.

3. Grease leakage. A sealed structure is needed to maintain the high durability of the gear and prevent grease leakage.

See the corresponding pages of the design guide of each series for “Recommended minimum housing clearance,” Application guide,” and “Application quantity.”
**Precautions on using Harmonic Grease® 4B No.2**

Harmonic Grease® 4B No.2 lubrication is ideally suited for Harmonic Drive® gears.

1. Apply the grease to each contacting joint at the beginning of operation.
2. Remove any contaminants created by abrasion during running-in period.

- See the corresponding pages of the design guide of each series for “recommended minimum housing clearance,” Application guide” and “Application quantity.”

**■ Precautions**

1. Stir Grease
   When storing Harmonic Grease 4B No.2 lubrication in the container, it is common for the oil to weep from the thickener. Before greasing, stir the grease in the container to mix and soften.

   (2) Aging (running-in)
   The aging before the main operation softens the applied grease. More effective greasing performance can be realized when the grease is distributed around each contact surface.
   Therefore, the following aging methods are recommended.
   - Keep the internal temperature at 80°C or cooler. Do not start the aging at high temperature rapidly.
   - Input rotational speed should be 1000rpm to 3000rpm. However, the lower rotational speed of 1000rpm is more effective.
   - Set the speed as low as possible within the indicated range.
   - The time required for aging is 20 minutes or longer.
   - Operation range for aging: Keep the output rotational angle as large as possible.

   Contact us if you have any questions for handling Harmonic Grease 4B No.2 lubrication.

   Note: Strict sealing is required to prevent grease leakage.

**Oil lubricant**

**■ Types of oil**

The specified standard lubricant is “Industrial gear oil class-2 (extreme pressure) ISO VG68.”

We recommend the following brands as a commercial lubricant.

<table>
<thead>
<tr>
<th>Standard</th>
<th>Mobil Oil</th>
<th>Exxon</th>
<th>Shell</th>
<th>COSMO Oil</th>
<th>Japan Energy</th>
<th>NIPPO Oil</th>
<th>Idemitsu Kosan</th>
<th>General Oil</th>
<th>Klüber</th>
</tr>
</thead>
<tbody>
<tr>
<td>Industrial gear oil class-2 (extreme pressure) ISO VG68</td>
<td>Mobilgear 600XP68</td>
<td>Spartan EP68</td>
<td>Omaha Oil 68</td>
<td>Cosmo gear SE68</td>
<td>ES gear G68</td>
<td>Bonock M68, Bonock AX68</td>
<td>Daphne super gear LW68</td>
<td>General Oil SP gear roll 68</td>
<td>Syntheso D-68EP</td>
</tr>
</tbody>
</table>

**■ When to replace oil**

First time ......................... 100 hours after starting operation
Second time or after ------- Every 1000 operation hours or every 6 months
Note that you should replace the oil earlier than specified if the operating condition is demanding.

- See the corresponding pages of the design guide of each series for specific details.

**■ Other precautions**

1. Avoid mixing different kinds of oil. The gear should be in an individual case when installed.

2. When you use size 50 or above at max allowable input speed, please contact us as it may cause lubrication problems.

* Oil lubrication is required for component-sets size 50 or larger with a reduction ratio of 50:1.
Lubricant for special environments

When the ambient temperature is special (other than the "temperature range of the operating environment" on Page 016-2), you should select a lubricant appropriate for the operating temperature range.

Harmonic Grease 4B No.2

Table 019-1

<table>
<thead>
<tr>
<th>Type of lubricant</th>
<th>Operating temperature range</th>
<th>Available temperature range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Grease</td>
<td>-10°C to + 110°C</td>
<td>-50°C to + 130°C</td>
</tr>
</tbody>
</table>

Harmonic Grease 4B No.2

Table 019-2

<table>
<thead>
<tr>
<th>Type of lubricant</th>
<th>Lubricant and manufacturer</th>
<th>Available temperature range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Grease</td>
<td>Mobil grease 28; Mobil Oil</td>
<td>-5°C to + 160°C</td>
</tr>
<tr>
<td>Oil</td>
<td>Mobil SHC-626; Mobil Oil</td>
<td>-5°C to + 140°C</td>
</tr>
</tbody>
</table>

Harmonic Grease 4B No.2

Table 019-3

<table>
<thead>
<tr>
<th>Type of lubricant</th>
<th>Lubricant and manufacturer</th>
<th>Available temperature range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Grease</td>
<td>Multemp SH-KII; Kyodo Oil</td>
<td>-30°C to + 50°C</td>
</tr>
<tr>
<td></td>
<td>Isoflex LDS-18 special A; KLÜBER</td>
<td>-25°C to + 80°C</td>
</tr>
<tr>
<td>Oil</td>
<td>SH-200-100CS; Toray Silicon</td>
<td>-40°C to + 140°C</td>
</tr>
<tr>
<td></td>
<td>Syntheso D-32EP; KLÜBER</td>
<td>-25°C to + 90°C</td>
</tr>
</tbody>
</table>

Harmonic Grease 4B No.2

The operating temperature range of Harmonic Grease 4B No.2 lubrication is the temperature at the lubricating section with the performance and characteristics of the gear taken into consideration. (It is not ambient temperature.)

As the available temperature range indicates the temperature of the independent lubricant, restriction is added on operating conditions (such as load torque, rotational speed and operating cycle) of the gear. When the ambient temperature is very high or low, materials of the parts of the gear need to be reviewed for suitability. Contact us if operating in high temperature.

Harmonic Grease 4B No.2 can be used in the available temperature range shown in table 019-1. However, input running torque will increase at low temperatures, and grease life will be decreased at high temperatures due to oxidation and lubricant degradation.
Torsional Stiffness

Stiffness and backlash of the drive system greatly affects the performance of the servo system. Please perform a detailed review of these items before designing your equipment and selecting a model number.

Stiffness

Fixing the input side (wave generator) and applying torque to the output side (flexspline) generates torsion almost proportional to the torque on the output side. Figure 018-1 shows the torsional angle at the output side when the torque applied on the output side starts from zero, increases up to \(+T_0\) and decreases down to \(-T_0\). This is called the “Torque – torsion angle diagram,” which normally draws a loop of 0 – A – B – A’ – B’ – A. The slope described in the “Torque – torsion angle diagram” is represented as the spring constant for the stiffness of the HarmonicDrive\textsuperscript{\textregistered} gear (unit: Nm/rad).

As shown in Figure 020-1, this “Torque – torsion angle diagram” is divided into 3 regions, and the spring constants in the area are represented by \(K_1\), \(K_2\) and \(K_3\).

- \(K_1\): The spring constant when the torque changes from [zero] to \([T_1]\)
- \(K_2\): The spring constant when the torque changes from \([T_1]\) to \([T_2]\)
- \(K_3\): The spring constant when the torque changes from \([T_2]\) to \([T_3]\)

Example for calculating the torsion angle

The torsion angle (\(\theta\)) is calculated here using CSF-2S-100-2A-GR as an example.

**When the applied torque is \(T_1\) or less, the torsion angle \(\theta_{1}\) is calculated as follows:**

When the load torque \(T_r := 2.9\) Nm

\[
\theta_{1} = \frac{T_r}{K_1} = \frac{2.9}{3.1 \times 10^3} = 9.4 \times 10^{-5}\text{ rad (0.33 arc min)}
\]

**When the applied torque is between \(T_1\) and \(T_2\), the torsion angle \(\theta_{2}\) is calculated as follows:**

When the load torque is \(T_r := 39\) Nm

\[
\theta_{2} = \frac{T_r}{K_2} = \frac{4.4 \times 10^{-4} + (39 - 14)/5.0 \times 10^3}{3.2 \text{ arc min}}
\]

When a bidirectional load is applied, the total torsion angle will be \(2 \times \theta_{x}\) plus hysteresis loss.

* The torsion angle calculation is for the gear component set only and does not include any torisonal windup of the input shaft.

Note: See p.120 for torsional stiffness for pancake gearing.

Hysteresis loss (Silk hat and cup style only)

As shown in Figure 020-1, when the applied torque is increased to the rated torque and is brought back to [zero], the torsional angle does not return exactly back to the zero point. This small difference (\(B - B'\)) is called hysteresis loss.

See the corresponding page of each series for the hysteresis loss value.

**Spring constant diagram**

**Backlash (Silk hat and cup style only)**

Hysteresis loss is primarily caused by internal friction. It is a very small value and will vary roughly in proportion to the applied load. Because HarmonicDrive\textsuperscript{\textregistered} gears have zero backlash, the only true backlash is due to the clearance in the Oldham coupling, a self-aligning mechanism used on the wave generator. Since the Oldham coupling is used on the input, the backlash measured at the output is extremely small (arc-seconds) since it is divided by the gear reduction ratio.
Positional Accuracy

Positional Accuracy values represent the difference between the theoretical angle and the actual angle of output for any given input. The values shown in the table are maximum values.

- See the corresponding pages of each series for transmission accuracy values.

Example of measurement

Graph 021-1

\[ \theta_{er} = \theta_i - \frac{\theta_i}{R} \]

Vibration

The primary frequency of the transmission error of the HarmonicDrive® gear may cause a vibration of the load inertia. This can occur when the driving frequency of the servo system including the HarmonicDrive® gear is at, or close to the resonant frequency of the system. Refer to the design guide of each series.

The primary component of the transmission error occurs twice per input revolution of the input. Therefore, the frequency generated by the transmission error is 2x the input frequency (rev / sec).

If the resonant frequency of the entire system, including the HarmonicDrive® gear, is \( f = 15 \) Hz, then the input speed (N) which would generate that frequency could be calculated with the formula below.

\[ N = \frac{15}{2} \cdot 60 = 450 \text{ rpm} \]

The resonant frequency is generated at an input speed of 450 rpm.
Starting Torque

Starting torque is the torque value applied to the input side at which the output first starts to rotate. The values in the table of each series indicate the maximum value, and the lower-limit value indicates approximately $\frac{1}{2}$ to $\frac{1}{3}$ of the maximum value.

**Measurement conditions:**
No-load, ambient temperature: +20°C

- See the corresponding pages of each series for starting torque values.

* Use the values in the table of each series as reference values as they vary depending on the usage conditions.

Backdriving Torque

Backdriving torque is the torque value applied to the output side at which the input first starts to rotate. The values in the table are maximum values, typical values are approximately $\frac{1}{2}$ of the maximum values.

Note: Never rely on these values as a margin in a system that must hold an external load. A brake must be used where back driving is not permissible.

**Measurement conditions:**
No-load, ambient temperature: +20°C

- See the corresponding pages of each series for backdriving torque values.

* Use the values in the table of each series as reference values as they vary depending on the usage conditions.
No-Load Running Torque

No-load running torque is the torque which is required to rotate the input side (high speed side), when there is no load on the output side (low speed side). The graph of the no-load running torque shown in this catalog depends on the measurement conditions shown in Table 023-1. Add the compensation values shown by each series to all reduction ratios except 100:1.

* See the corresponding pages of each series for no-load running torque values.

Efficiency

The efficiency varies depending on the following conditions:
- Reduction ratio
- Input speed
- Load torque
- Temperature
- Lubrication (type and quantity)

The efficiency characteristics of each series shown in this catalog depends on the measurement condition shown in Table 023-2.

* See the corresponding pages of each series for efficiency values.

**Efficiency compensation coefficient**

If load torque is below rated torque, a compensation factor must be employed. Calculate the compensation coefficient Ke from the efficiency compensation coefficient graph of each series and use the following example for calculation.

**Example of calculation**

Efficiency  $\eta$ (%) under the following condition is obtained from the example of CSF-20-80-2A-GR.

- Input rotational speed: 1000 rpm
- Load torque: 19.6 Nm
- Lubrication method: Grease lubrication (Harmonic Grease SK-1A)
- Lubricant temperature: 20°C

Since the rated torque of size 20 with a reduction ratio of 80 is 34 Nm (Ratings: Page 039), the torque ratio $\alpha$ is 0.58. ($\alpha=19.6/34=0.58$)

* The efficiency compensation coefficient is $Ke=0.93$ from Graph 023-1.
* Efficiency $\eta$ at load torque 19.6 Nm: $\eta=Ke \cdot \eta_R=0.93 \times 78=73\%$

* Contact us for oil lubrication.
Design Guidelines

Design guideline

The relative perpendicularity and concentricity of the three basic Harmonic Drive® elements have an important influence on accuracy and service life.

Misalignments will adversely affect performance and reliability. Compliance with recommended assembly tolerances is essential in order for the advantages of Harmonic Drive® gearing to be fully realized. Please consider the following when designing:

(1) Input shaft, Circular Spline and housing must be concentric.

(2) When operating, an axial force is generated on the wave generator. Input bearings must be selected to accommodate this axial load. See page 27.

(3) Even though a HarmonicDrive® gear is compact, it transmits large torques. Therefore, assure that all required bolts are used to fasten the circular spline and flexspline and that they are tightened to the recommended torque.

(4) As the flexspline is subject to elastic deformation, a minimal clearance between the flexspline and housing is required. Refer to "Minimum Housing Clearance" on the drawing dimension tables.

(5) The input shaft and output shaft are supported by anti-friction bearings. As the wave generator and flexspline elements are meant to transmit pure torque only, the bearing arrangement needs to isolate the harmonic gearing from external forces applied to either shaft. A common bearing arrangement is depicted in the diagram.

(6) A clamping plate is recommended (item 6). Its purpose is to spread fastening forces and to avoid any chance of making physical contact with the thin section of the flexspline diaphragm. The clamping plate shall not exceed the diaphragm’s boss diameter and is to be designed in accordance with catalog recommendations.

Fig. 024-1
Bearing support for the input and output shafts

For the component sets, both input and output shafts must be supported by two adequately spaced bearings in order to withstand external radial and axial forces without excessive deflection. In order to avoid damage to the component set when limited external loads are anticipated, both input and output shafts must be axially fixed.

Bearings must be selected whose radial play does not exceed ISO-standard C 2 class or “normal” class. The bearings should be axially and radially preloaded to eliminate backlash. Examples of correct bearing arrangements are shown in fig 025-1.
Wave generator

Structure of the wave generator

The wave generator includes an Oldham’s coupling type with a self-aligning structure and an integrated solid wave generator without a self-aligning structure, and which is used depends on the series. See the diagram of each series for details. The basic structure of the wave generator and the shape are shown below.

![Diagram of Wave Generator Components](image-url)

- Ball Separator
- Wave generator bearing
- Wave generator plug
- Insert
- Rubwasher
- Snap ring
- Wave generator hub

Structure of Oldham’s coupling

![Diagram of Oldham’s Coupling](image-url)
Maximum hole diameter of wave generator

The standard hole dimension of the wave generator is shown for each size. The dimension can be changed within a range up to the maximum hole dimension. We recommend the dimension of keyway based on JIS standard. It is necessary that the dimension of keyways should sustain the transmission torque. * Tapered holes are also available.

In cases where a larger hole is required, use the wave generator without the Oldham coupling. The maximum diameter of the hole should be considered to prevent deformation of the Wave Generator plug by load torque. The dimension is shown in the table below and includes the dimension of depth of keyway. (This is the value including the dimension of the depth of keyway.)

Hole diameter of the wave generator hub with Oldham coupling

<table>
<thead>
<tr>
<th>Size</th>
<th>8</th>
<th>11</th>
<th>14</th>
<th>17</th>
<th>20</th>
<th>25</th>
<th>32</th>
<th>40</th>
<th>45</th>
<th>50</th>
<th>58</th>
<th>65</th>
<th>80</th>
<th>90</th>
<th>100</th>
</tr>
</thead>
<tbody>
<tr>
<td>Standard dim. (H7)</td>
<td>3</td>
<td>5</td>
<td>6</td>
<td>8</td>
<td>9</td>
<td>11</td>
<td>14</td>
<td>14</td>
<td>19</td>
<td>19</td>
<td>22</td>
<td>24</td>
<td>28</td>
<td>28</td>
<td>28</td>
</tr>
<tr>
<td>Minimum hole dim.</td>
<td>—</td>
<td>—</td>
<td>3</td>
<td>4</td>
<td>5</td>
<td>6</td>
<td>6</td>
<td>10</td>
<td>10</td>
<td>13</td>
<td>16</td>
<td>16</td>
<td>19</td>
<td>22</td>
<td>22</td>
</tr>
<tr>
<td>Maximum hole dim.</td>
<td>—</td>
<td>—</td>
<td>8</td>
<td>10</td>
<td>13</td>
<td>15</td>
<td>15</td>
<td>20</td>
<td>20</td>
<td>25</td>
<td>30</td>
<td>35</td>
<td>37</td>
<td>40</td>
<td>40</td>
</tr>
</tbody>
</table>

Maximum hole diameter without Oldham Coupling

<table>
<thead>
<tr>
<th>Size</th>
<th>8</th>
<th>11</th>
<th>14</th>
<th>17</th>
<th>20</th>
<th>25</th>
<th>32</th>
<th>40</th>
<th>45</th>
<th>50</th>
<th>58</th>
<th>65</th>
<th>80</th>
<th>90</th>
<th>100</th>
</tr>
</thead>
<tbody>
<tr>
<td>Max. hole dia.</td>
<td>10</td>
<td>14</td>
<td>17</td>
<td>20</td>
<td>23</td>
<td>28</td>
<td>36</td>
<td>42</td>
<td>47</td>
<td>52</td>
<td>60</td>
<td>67</td>
<td>72</td>
<td>84</td>
<td>95</td>
</tr>
<tr>
<td>Min. plug thick</td>
<td>5.7</td>
<td>6.7</td>
<td>7.2</td>
<td>7.6</td>
<td>11.3</td>
<td>11.3</td>
<td>13.7</td>
<td>15.9</td>
<td>17.8</td>
<td>19</td>
<td>21.4</td>
<td>23.5</td>
<td>28.5</td>
<td>31.3</td>
<td>34.9</td>
</tr>
</tbody>
</table>

Axial Force of Wave Generator

When the gear is used to accelerate a load, the deflection of the Flexspline leads to an axial force acting on the Wave Generator. This axial force, which acts in the direction of the closed end of the Flexspline, must be supported by the bearings of the input shaft (motor shaft). When the gear is used to decelerate a load, an axial force acts to push the Wave Generator out of the Flexspline cup. Maximum axial force of the Wave Generator can be calculated by the equation shown below. The axial force may vary depending on its operating condition. The value of axial force tends to be a larger number when using high torque, extreme low speed and constant operation. The force is calculated (approximately) by the equation. In all cases, the Wave Generator must be axially (in both directions), as well as torsionally, fixed to the input shaft.

(Note) Please contact us for further information on attaching the Wave Generator to the input (motor) shaft.

Formula for Axial Force

<table>
<thead>
<tr>
<th>Reduction ratio</th>
<th>Calculation formula</th>
</tr>
</thead>
<tbody>
<tr>
<td>30</td>
<td>$F=2\times \frac{D \times 0.07 \times \tan 32°}{N}$</td>
</tr>
<tr>
<td>50</td>
<td>$F=2\times \frac{D \times 0.07 \times \tan 30°}{N}$</td>
</tr>
<tr>
<td>80 or more</td>
<td>$F=2\times \frac{D \times 0.07 \times \tan 20°}{N}$</td>
</tr>
</tbody>
</table>

Symbols for Formula

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>F</td>
<td>Axial force</td>
</tr>
<tr>
<td>N</td>
<td>See Figure 027-2</td>
</tr>
<tr>
<td>D</td>
<td>Size (mm)</td>
</tr>
<tr>
<td>T</td>
<td>Output torque (Nm)</td>
</tr>
</tbody>
</table>
## Assembly Precautions

### Sealing
Sealing is needed to maintain the high durability of the gear and prevent grease leakage. Recommended for all mating surfaces, if the o-ring is not used. Flanges provided with o-ring grooves must be sealed when a proper seal cannot be achieved using the o-ring alone.

- **Rotating Parts** — Oil seal with spring is needed.
- **Mating flange** — O-ring or seal adhesive is needed.
- **Screw hole area** — Screws should have a thread lock (LOCTITE® 242 is recommended) or seal adhesive.

(Note) If you use Harmonic Grease 4BNo.2, strict sealing is required.

### Assembly precautions
The wave generator is installed after the flexspline and circular spline. If the wave generator is not inserted into the flexspline last, gear teeth scuffing damage or improper eccentric gear mesh may result. Installation resulting in an eccentric tooth mesh (Dedoidal) will cause noise and vibration, and can lead to early failure of the gear. For proper function, the teeth of the flexspline and Circular Spline mesh symmetrically.

#### Precautions on the wave generator
1. Avoid applying undue axial force to the wave generator during installation. Rotating the wave generator bearing while inserting it is recommended and will ease the process.
2. If the wave generator does not have an Oldham coupling, extra care must be given to ensure that concentricity and inclination are within the specified limits.

#### Precautions on the circular spline
The circular Spline must not be deformed in any way during the assembly. It is particularly important that the mounting surfaces are prepared correctly.

1. Mounting surfaces need to have adequate flatness, smoothness, and no distortion.
2. Especially in the area of the screw holes, burrs or foreign matter should not be present.
3. Adequate relief in the housing corners is needed to prevent interference with the corner of the circular spline.
4. The circular spline should be rotatable within the housing. Be sure there is no interference and that it does not catch on anything.
5. When a bolt is inserted into a bolt hole during installation, make sure that the bolt fits securely and is not in an improper position or inclination.
6. Do not apply torque at recommended torque all at once. First, apply torque at about half of the recommended value to all bolts, then tighten at recommended torque. Order of tightening bolts must be diagonal.
7. Avoid pinning the circular spline if possible as it can reduce the rotational precision and smoothness of operation.

#### Precautions on the flexspline
1. Mounting surfaces need to have adequate flatness, smoothness, and no distortion.
2. Especially in the area of the screw holes, burrs or foreign matter should not be present.
3. Adequate clearance with the housing is needed to ensure no interference especially with the major axis of flexspline.
4. Bolts should rotate freely when installing through the mounting holes of the flexspline and should not have any irregularity due to the shaft bolt holes being misaligned or oblique.
5. Do not tighten the bolts with the specified torque all at once. Tighten the bolts temporarily with about half the specified torque, and then tighten them to the specified torque. Tighten them in an even, crisscross pattern.
6. The flexspline and circular spline are concentric after assembly. After installing the wave generator bearing, if it rotates in unbalanced way, check the mounting for dedoidal or non-concentric installation.
7. Care should be taken not to damage the flexspline diaphragm or gear teeth during assembly. Avoid hitting the tips of the flexspline teeth and circular spline teeth. Avoid installing the CS from the open side of the flexspline after the wave generator has been installed.

#### Rust prevention
Although the Harmonic Drive® gears come with some corrosion protection, the gear can rust if exposed to the environment. The gear external surfaces typically have only a temporary corrosion inhibitor and some oil applied. If an anti-rust product is needed, please contact us to review the options.

### Sealing recommendations for gear units

<table>
<thead>
<tr>
<th>Area requiring sealing</th>
<th>Recommended sealing method</th>
</tr>
</thead>
<tbody>
<tr>
<td>Output side</td>
<td></td>
</tr>
<tr>
<td>Holes which penetrate housing</td>
<td>Use O-ring (supplied with the product)</td>
</tr>
<tr>
<td>Installation screw / bolt</td>
<td>Screw lock adhesive which has effective seal (LOCTITE® 242 is recommended)</td>
</tr>
<tr>
<td>Input side</td>
<td></td>
</tr>
<tr>
<td>Flange surfaces</td>
<td>Use O-ring (supplied with the product)</td>
</tr>
<tr>
<td>Motor output shaft</td>
<td>Please select a motor which has an oil seal on the output shaft.</td>
</tr>
</tbody>
</table>
"Dedoidal" state

It is normal for the flexspline to engage with the circular spline symmetrically as shown in Figure 029-1. However, if the ratcheting phenomenon, which is described on Page 013, is caused or if the three parts are forcibly inserted and assembled, engagement of the teeth may be out of alignment as shown in Figure 029-2. This is called "dedoidal". Note: Early failure of the gear will occur.

■ How to check "dedoidal"

By performing the following methods, check whether the gear engagement is "dedoidal".

1. Judging by the irregular torque generated when the wave generator turns
   1) Slowly turn the input shaft with your hand in a no-load condition. If you can turn it with average force, it is normal. If it turns irregularly, it may be "dedoidal".
   2) Turn the wave generator in a no-load condition if it is attached to a motor. If the average current value of the motor is about 2 to 3 times the normal value, it may be "dedoidal".

2. Judging by measuring vibration on the body of the flexspline
   The scale deflection of the dial gauge draws a sine wave as shown by the solid line in Graph 029-3 when it is normally assembled. When "dedoidal" occurs, the gauge draws a deflected wave shown by the dotted line as the flexspline is out of alignment.
Checking Output Bearing

A precision cross roller bearing is built in the unit type and the gear head type to directly support the external load (output flange) (precision 4-point contact ball bearing for the CSF-mini series). Please calculate maximum moment load, life of cross roller bearing, and static safety factor to fully maximize the performance of a housed unit (gearhead).

See the corresponding pages on each series for cross roller bearing specifications.

Checking procedure

1. Checking the maximum moment load ($M_{\text{max}}$)
   - Calculate maximum moment load ($M_{\text{max}}$).
   - Maximum moment load ($M_{\text{max}}$) ≤ allowable moment ($M_c$)

2. Checking the life
   - Calculate the radial load ($F_{\text{rad}}$) and the average axial load ($F_{\text{avg}}$).
   - Calculate the radial load coefficient ($x$) and the axial load coefficient ($y$).
   - Calculate the life.

3. Checking the static safety coefficient
   - Calculate the static equivalent radial load coefficient ($P_o$).
   - Check the static safety coefficient ($f_s$).

How to calculate the maximum moment load

Maximum moment load ($M_{\text{max}}$) is obtained as follows. Make sure that $M_{\text{max}} \leq M_c$.

$$M_{\text{max}} = F_{\text{rad}} (L_r + R) + F_{\text{avg}} \cdot L_a$$

Symbols for Formula 030-1

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>$F_{\text{rad}}$</td>
<td>Max. radial load</td>
<td>N(kgf)</td>
</tr>
<tr>
<td>$F_{\text{avg}}$</td>
<td>Max. axial load</td>
<td>N(kgf)</td>
</tr>
<tr>
<td>$L_r, L_a$</td>
<td>Offset amount</td>
<td>m</td>
</tr>
<tr>
<td>$R$</td>
<td>Offset amount</td>
<td>m</td>
</tr>
</tbody>
</table>

See Fig. 030-1 and “Specification of the output bearing” of each series.
How to calculate the average load

(Average radial load, average axial load, average output speed)
When the radial load and axial load vary, the life of cross roller bearing can be determined by converting to an average load.

1. **How to calculate the average radial load \((F_{r\text{av}})\)**
   - **(Cross roller bearing)**
     \[
     F_{r\text{av}} = \sqrt{\frac{n_1 t_1 (F_{r1})^{\alpha_1} + n_2 t_2 (F_{r2})^{\alpha_2} + \ldots + n_n t_n (F_{rn})^{\alpha_n}}{n_1 t_1 + n_2 t_2 + \ldots + n_n t_n}}
     \]
   - **(4-point contact ball bearing)**
     \[
     F_{r\text{av}} = \sqrt{\frac{n_1 t_1 (F_{r1})^{\alpha_1} + n_2 t_2 (F_{r2})^{\alpha_2} + \ldots + n_n t_n (F_{rn})^{\alpha_n}}{n_1 t_1 + n_2 t_2 + \ldots + n_n t_n}}
     \]
   Note that the maximum radial load in \(t_1\) is \(F_{r1}\) and the maximum radial load in \(t_n\) is \(F_{rn}\).

2. **How to calculate the average axial load \((F_{a\text{av}})\)**
   - **(Cross roller bearing)**
     \[
     F_{a\text{av}} = \sqrt{\frac{n_1 t_1 (F_{a1})^{\alpha_1} + n_2 t_2 (F_{a2})^{\alpha_2} + \ldots + n_n t_n (F_{an})^{\alpha_n}}{n_1 t_1 + n_2 t_2 + \ldots + n_n t_n}}
     \]
   - **(4-point contact ball bearing)**
     \[
     F_{a\text{av}} = \sqrt{\frac{n_1 t_1 (F_{a1})^{\alpha_1} + n_2 t_2 (F_{a2})^{\alpha_2} + \ldots + n_n t_n (F_{an})^{\alpha_n}}{n_1 t_1 + n_2 t_2 + \ldots + n_n t_n}}
     \]
   Note that the maximum axial load in \(t_1\) is \(F_{a1}\) and the maximum axial load in \(t_n\) is \(F_{an}\).

3. **How to calculate the average output speed \((N_{av})\)**
   \[
   N_{av} = \frac{n_1 t_1 + n_2 t_2 + \ldots + n_n t_n}{t_1 + t_2 + \ldots + t_n}
   \]

**How to calculate the radial load coefficient \((X)\) and axial load coefficient \((Y)\)**

### Table 031-1

<table>
<thead>
<tr>
<th>Formula 031-4</th>
<th>X</th>
<th>Y</th>
</tr>
</thead>
<tbody>
<tr>
<td>(F_{r\text{av}})</td>
<td>(&lt;=1.5)</td>
<td>1</td>
</tr>
<tr>
<td>(F_{r\text{av}} + 2 (F_{r\text{av}} (L_{r\text{a}} + R) + F_{a\text{av}} L_{a}) / dp)</td>
<td>&gt;1.5</td>
<td>0.67</td>
</tr>
</tbody>
</table>

**Symbols for Formula 031-4**

- \(F_{r\text{av}}\): Average radial load (N(kgf))
- \(F_{a\text{av}}\): Average axial load (N(kgf))
- \(L_{r\text{a}}, L_{a}\): Offset amount (m)
- \(R\): Pitch circle diameter of a roller (m)
- \(dp\): See "How to calculate the average load.* See Formula 031-1.
- See Fig. 030-1 and "Main roller bearing specifications" of each series.

*See "How to calculate the average load.* See Formula 031-1.
Life of the output bearing

Calculate life of the output bearing by Formula 032-1. You can calculate the dynamic equivalent radial load (Pc) by Formula 032-2.

Formula 032-1

\[
L_{10} = \frac{10^7}{60 \times N_{av}} \times \left( \frac{C}{f_{w} \cdot P_c} \right)^{3/2}
\]

Formula 032-2

\[
P_c = X \cdot \left( \frac{F_{rav} + \frac{2(F_{rav} \cdot L_r + F_{av} \cdot L_a)}{dp}}{Y \cdot F_{av}} \right)
\]

Symbols for Formula 032-1

<table>
<thead>
<tr>
<th>L_{10}</th>
<th>Life</th>
<th>hour</th>
<th>---</th>
</tr>
</thead>
<tbody>
<tr>
<td>N_{av}</td>
<td>Average output rated load speed</td>
<td>rpm</td>
<td>See “How to calculate the average load.”</td>
</tr>
<tr>
<td>C</td>
<td>Basic dynamic rated load</td>
<td>N (kgf)</td>
<td>See “Specification of the output bearing” of each series.</td>
</tr>
<tr>
<td>P_c</td>
<td>Dynamic equivalent load</td>
<td>N (kgf)</td>
<td>See Formula 032-2.</td>
</tr>
<tr>
<td>f_{w}</td>
<td>Load coefficient</td>
<td>---</td>
<td>See Table 032-3.</td>
</tr>
</tbody>
</table>

Symbols for Formula 032-2

| F_{rav} | Average radial load | N (kgf) | See “How to calculate the average load.” See Formula 031-1. |
| F_{av}  | Average axial load | N (kgf) | See “How to calculate the average load.” See Formula 031-2. |
| dp      | Pitch circle diameter | m | See Fig. 030-1 and “Specification of the output bearing” of each series. |
| X       | Radial load coefficient | --- | See Formula 031-4. |
| Y       | Axial load coefficient | --- | See Formula 031-4. |
| L_r, L_a| Offset | m | See Figure 030-1. |
| R       | Offset | m | See Fig. 030-1 and “Specification of the output bearing” of each series. |
| M_{ave} | Average moment load | Nm | |

Load coefficient

<table>
<thead>
<tr>
<th>Load status</th>
<th>f_{w}</th>
</tr>
</thead>
<tbody>
<tr>
<td>Steady operation without impact and vibration</td>
<td>1 to 1.2</td>
</tr>
<tr>
<td>Normal operation</td>
<td>1.2 to 1.5</td>
</tr>
<tr>
<td>Operation with impact and vibration</td>
<td>1.5 to 3</td>
</tr>
</tbody>
</table>
How to calculate life during oscillating motion

Calculate the life of the cross roller bearing during oscillating motion by Formula 033-1.

\[
\text{Loc} = \frac{10^6}{60 \times n1} \times \frac{90}{\theta} \times \left( \frac{C}{f\text{w} \times \text{Pc}} \right)^{\frac{3}{2}}
\]

(Cross roller bearing)

\[
\text{Loc} = \frac{10^6}{60 \times n1} \times \frac{90}{\theta} \times \left( \frac{C}{f\text{w} \times \text{Pc}} \right)^{\frac{3}{2}}
\]

(4-point contact ball bearing)

**Symbols for Formula 033-1**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Loc</td>
<td>Rated life for oscillating motion (hr)</td>
</tr>
<tr>
<td>n1</td>
<td>Round trip oscillation each minute (rpm)</td>
</tr>
<tr>
<td>C</td>
<td>Basic dynamic rated load (N/\text{kgf})</td>
</tr>
<tr>
<td>Pc</td>
<td>Dynamic equivalent radial load (N/\text{kgf})</td>
</tr>
<tr>
<td>fw</td>
<td>Load coefficient</td>
</tr>
<tr>
<td>(\theta)</td>
<td>Oscillating angle/2 (Degree)</td>
</tr>
</tbody>
</table>

**Table 033-1**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Loc</td>
<td>Rated life for oscillating motion (hr)</td>
</tr>
<tr>
<td>n1</td>
<td>Round trip oscillation each minute (rpm)</td>
</tr>
<tr>
<td>C</td>
<td>Basic dynamic rated load (N/\text{kgf})</td>
</tr>
<tr>
<td>Pc</td>
<td>Dynamic equivalent radial load (N/\text{kgf})</td>
</tr>
<tr>
<td>fw</td>
<td>Load coefficient</td>
</tr>
<tr>
<td>(\theta)</td>
<td>Oscillating angle/2 (Degree)</td>
</tr>
</tbody>
</table>

(Note) A small angle of oscillation (less than 5 degrees) may cause fretting corrosion to occur since lubrication may not circulate properly. Contact us if this happens.
How to calculate the static safety coefficient

Basic static rated load is an allowable limit for static load, but its limit is determined by usage. In this case, static safety coefficient of the cross roller bearing can be calculated by Formula 034-2.

\[
fs = \frac{Co}{Po}
\]

\[
Po = Fr_{max} + \frac{2M_{max}}{dp} + 0.44Fa_{max}
\]

**Symbols for Formula 034-1**

<table>
<thead>
<tr>
<th>Co</th>
<th>Basic static rated load N(kgf)</th>
<th>See “Specification of the output bearing” of each series.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Po</td>
<td>Static equivalent radial load N(kgf)</td>
<td>See Formula 034-2.</td>
</tr>
</tbody>
</table>

**Symbols for Formula 034-2**

| Fr_{max} | Max. radial load N(kgf) | See “Specification of the output bearing” of each series. |
| Fan_{max} | Max. axial load N(kgf) | |
| M_{max} | Max. moment load Nm(kgfm) | |
| dp | Pitch circle diameter of a roller m | See Fig. 030-1 and “Specification of the output bearing” of each series. |

**Table 034-1**

<table>
<thead>
<tr>
<th>Operating condition of the roller bearing</th>
<th>fs</th>
</tr>
</thead>
<tbody>
<tr>
<td>When high rotation precision is required</td>
<td>≥3</td>
</tr>
<tr>
<td>When shock and vibration are expected</td>
<td>≥2</td>
</tr>
<tr>
<td>Under normal operating condition</td>
<td>≥1.5</td>
</tr>
</tbody>
</table>
HarmonicDrive® Reducer for Precision Control

For Safe Use of Harmonic Drive® Component Set and Gear Unit

**Warning**: Means that improper use or handling could result in a risk of death or serious injury.

**Caution**: Means that improper use or handling could result in personal injury or damage to property.

**Limited Applications**

This product cannot be used for the following applications:

- Space equipment
- Aircraft equipment
- Medical equipment
- Nuclear power equipment
- Game equipment
- Equipment and apparatus used in domestic homes
- Equipment that directly works on human bodies
- Equipment for transport of humans
- Equipment for use in a special environment

Please consult Harmonic Drive beforehand when intending to use one of its product for the aforementioned applications.

Install a safety device that avoids an accident even if output of this product becomes uncontrollable due to breakdown when using it in equipment that affects human lives and that may trigger serious damage.

**Design Precaution**: Be certain to read the catalog when designing your equipment.

- Use only in a specified environment.
  - Please ensure the following environmental conditions are complied with:
    - Ambient temperature 0 to 40°C
    - No splashing of water or oil
    - No dust such as metal powder

- Install the equipment in a specified manner.
  - Carry out assembly precisely in the specified order according to the catalog.
  - Observe our recommended tightening methods (such as bolts used).
  - Operating the equipment without precise assembly can cause troubles such as generation of vibration, reduction of life, deterioration of precision and breakdown.

- Install the equipment in a specified precision.
  - Design and assemble parts to maintain the recommended installation and assembly tolerances in the catalog.
  - Failure to keep the precision can cause troubles such as vibration, reduction of life, deterioration of precision and breakdown.

- Use the specified lubricant.
  - Using other lubricant than our recommended products can reduce the life. Replace the lubricant in a specified condition.
  - Grease is sealed in a unit product. Do not mix other kinds of grease.

**Operational Precaution**: Be certain to read the catalog before operating the equipment.

- Be careful in handling products and parts.
  - Do not impact the parts and units with a hammer, etc. Do not scratch or dent them. Possible damage is assumed.
  - If you use the equipment in a damaged condition, the specified performance may not be retained. It can also cause troubles such as breakdown.

- Apply torque within the allowable range.
  - Do not apply torque exceeding the instantaneous allowable max. torque. Applying excess torque can cause troubles such as loose tightening bolts, generation of backlash and breakdown.
  - Sinking an arm directly attached to the output shaft can damage the arm and make the output shaft uncontrollable.

- Do not change a set of parts.
  - The product is manufactured with matched serial numbers. The specified performance may not be retained if you have used mixed sets of parts.

- Do not break down unit products.
  - Do not break down and reassemble unit products. Original performance may not be reproduced.

- Do not break down unit products.
  - Do not break down and reassemble unit products. Original performance may not be reproduced.

- Rust-proofing was applied before shipping. However, please note that rusting occurs earlier depending on the customers' storage environment.
  - Although black oxide finish is applied to some of our products, it dose not guarantee the antirust effect.

**Handling lubricant**

- Precautions on handling lubricant
  - Use protective eyewear when handling. Avoid contact with eyes. May cause inflammation.
  - Use gloves and other skin protection when handling. Avoid contact with skin. May cause inflammation.
  - Do not swallow. May cause diarrhea and vomiting.
  - Keep out of reach of children.

- Treatment of waste oil and containers
  - Proper disposal is essential. Dispose of waste oil and waste containers properly in accordance with applicable laws and regulations.
  - Do not apply pressure on an empty container.
  - Do not weld, heat, drill or cut the container. The remainder may ignite with an explosion.

- First-aid
  - EYES: Flush with clean water for at least 15 minutes. Consult a physician.
  - SKIN: Thoroughly remove with cloth or paper and wash with soap and water.
  - INGESTION: Consult a physician immediately. Do not induce vomiting.
  - INHALATION: Immediately seek fresh air if adverse effects are observed.

- Storage
  - Close the container tightly after use in order to prevent contamination with dust or moisture. Avoid direct exposure to sunlight. Store at room temperature.

- When Discarding Actuator and Servo Driver
  - Please discard as industrial waste.

---

**Component**
Group Companies
Harmonic Drive Systems, Inc.
6-25-3 Minami-Ohi, Shinagawa-ku
Tokyo 141-0013, Japan

Harmonic Drive AG
Hoembergstrasse, 14, D-655
Limburg/Lahn Germany

Harmonic Drive®, Harmonic Gearhead®, Harmonic Planetary® and Quick Connect® are registered trademarks of Harmonic Drive LLC. All other trademarks are property of their respective owners.