

# HarmonicDrive®

## CSF-GH Standard Series

### Size

14, 20, 32, 45, 65

**5**  
Sizes

### Peak torque

18Nm to 2630Nm

### Reduction ratio

50:1 to 160:1

### Zero backlash

### High Accuracy

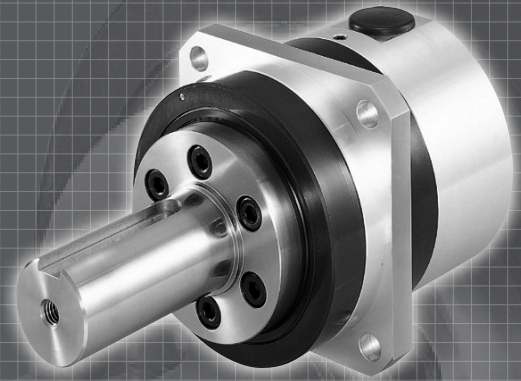
Repeatability  $\pm 4$  to  $\pm 10$  arc-sec

### High Load Capacity Output Bearing

A Cross Roller bearing is integrated with the output flange to provide high moment stiffness, high load capacity and precise positioning accuracy.

### Easy mounting to a wide variety of servomotors

Quick Connect™ coupling



## CONTENTS

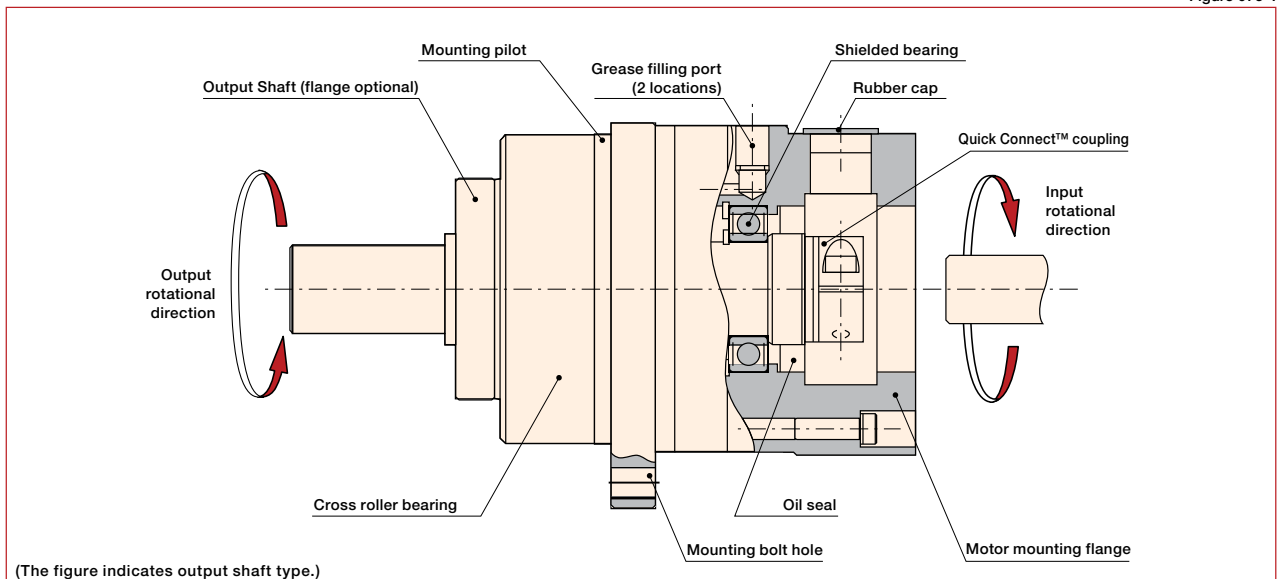
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## CSF - 20 - 100 - GH - F0 Motor Model Number

Model Name	Size	Reduction Ratio	Model	Output Configuration	Input Configuration
HarmonicDrive® CSF Standard	14	50, 80, 100	GH: Gearhead	F0: Flange output J2: Straight shaft (without key) J6: Straight shaft (with key and center tapped hole)	This code represents the motor mounting configuration. Please contact us for a unique part number based on the motor you are using.
	20	50, 80, 100, 120, 160			
	32				
	45				
	65	80, 100, 120, 160			

### Gearhead Construction

Figure 076-1



## Rating Table CSF-GH

Table 077-1

Size	Ratio	Rated output torque at 2000 rpm <sup>*1</sup>	Rated output torque at 3000 rpm <sup>*2</sup>	Limit for Average Torque <sup>*3</sup>	Limit for Repeated Peak Torque <sup>*4</sup>	Limit for Momentary Torque <sup>*5</sup>	Max. Input Speed <sup>*6</sup>	Mass <sup>*7</sup>	
		Nm	Nm	Nm	Nm	Nm	rpm	Shaft	Flange
								kg	kg
14	50	5.4	4.7	6.9	18	35	8500	0.62	0.50
	80	7.8	6.8	11	23	47			
	100	7.8	6.8	11	28	54			
20	50	25	22	34	56	98	6500	1.8	1.4
	80	34	30	47	74	127			
	100	40	35	49	82	147			
	120	40	35	49	87	147			
	160	40	35	49	92	147			
32	50	76	66	108	216	382	4800	4.6	3.2
	80	118	103	167	304	568			
	100	137	120	216	333	647			
	120	137	120	216	353	686			
	160	137	120	216	372	686			
45	50	176	154	265	500	950	3800	13	10
	80	313	273	390	706	1270			
	100	353	308	500	755	1570			
	120	402	351	620	823	1760			
	160	402	351	630	882	1910			
65	80	745	651	1040	2110	3720	2800	32	24
	100	951	831	1520	2300	4750			
	120	951	831	1570	2510	4750			
	160	951	831	1570	2630	4750			

\*1: Rated torque is based on L10 life of 7,000 hours when input speed is 2000 rpm

\*2: Rated torque is based on L10 life of 7,000 hours when input speed is 3000 rpm, input speed for size 65 is 2800 rpm.

\*3: Maximum value of average load torque is based on the load torque pattern. Note that exceeding this value may deteriorate the life or durability of the product.

\*4: The limit for torque during start and stop cycles.

\*5: The limit for torque during emergency stops or from external shock loads. Always operate below this value. Calculate the number of permissible events to ensure it meets required operating conditions.

\*6: Maximum instantaneous input speed.

\*7: The mass is for the gearhead only (without input shaft coupling & motor flange). Please contact us for the mass of your specific configuration.

\*8: See page 86 for more information on torque ratings.

## Ratcheting Torque CSF-GH

(Unit: Nm) Table 077-2

Size	14	20	32	45	65
Reduction ratio					
50	88	220	980	2700	—
80	110	350	1400	3900	11000
100	84	260	1000	3100	9400
120	—	240	980	2800	8300
160	—	220	980	2600	8000

## Buckling Torque CSF-GH

(Unit: Nm) Table 077-3

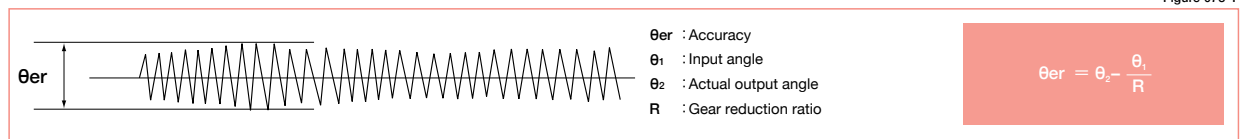
Size	14	20	32	45	65
All Ratios	190	560	2200	5800	17000

# Performance Table CSF-GH

Table 078-1

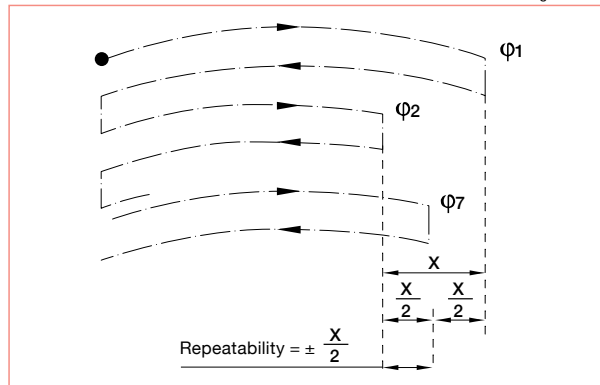
Size	Flange Type	Ratio	Accuracy <sup>*1</sup>		Repeatability <sup>*2</sup>	Starting torque <sup>*3</sup>		Backdriving torque <sup>*4</sup>		No-load running torque <sup>*5</sup>	
			arc min	x10 <sup>-4</sup> rad		Ncm	kgfcm	Nm	kgfm	Ncm	kgfcm
14	All	50	1.5	4.4	±10	8.2	0.8	2.9	0.3	5.6	0.6
		80				6.9	0.7	3.9	0.4	5.1	0.5
		100				6.6	0.7	4.7	0.5	4.6	0.5
20	Type I	50	1.0	2.9	±8	13	1.3	7.8	0.8	11	1.2
		80				10	1.0	9.6	1.0	10	1.0
		100				9.6	1.0	12	1.2	10	1.0
		120				9.1	0.9	13	1.3	9.8	1.0
		160				8.6	0.9	17	1.7	9.6	1.0
	Type II	50	1.0	2.9	±8	20	2.0	12	1.2	11	1.2
		80				17	1.7	16	1.6	10	1.0
		100				16	1.7	19	2.0	10	1.0
		120				16	1.6	23	2.3	9.8	1.0
		160				15	1.6	29	3.1	9.6	1.0
32	Type I & II	50	1.0	2.9	±6	58	5.9	35	3.6	47	4.8
		80				46	4.7	44	4.5	42	4.3
		100				45	4.6	54	5.5	41	4.2
		120				42	4.3	61	6.2	40	4.1
		160				41	4.2	79	8.1	40	4.1
	Type III	50	1.0	2.9	±6	50	5.1	30	3.1	47	4.8
		80				38	3.9	37	3.8	42	4.3
		100				37	3.8	45	4.6	41	4.2
		120				34	3.5	49	5.1	40	4.1
		160				33	3.4	64	6.6	40	4.1
45	All	50	1.0	2.9	±5	123	13	74	7.8	120	12
		80				95	9.7	92	9.3	109	11
		100				89	9.1	107	11	107	11
		120				85	8.7	123	13	105	11
		160				79	8.1	152	16	103	11
65	All	80	1.0	2.9	±4	186	19	179	18	297	30
		100				166	17	200	20	289	30
		120				156	16	226	23	285	29
		160				139	14	268	27	278	28

\*1: Accuracy values represent the difference between the theoretical angle and the actual angle of output for any given input. The values shown in the table are maximum values.



\*2: The repeatability is measured by moving to a given theoretical position seven times, each time approaching from the same direction. The actual position of the output shaft is measured each time and repeatability is calculated as the 1/2 of the maximum difference of the seven data points. Measured values are indicated in angles (arc-sec) prefixed with "±". The values in the table are maximum values.

Figure 078-2



\*3: Starting torque is the torque value applied to the input side at which the output first starts to rotate. The values in the table are maximum values.

Table 078-2

Load	No load
Speed reducer surface temperature	25°C

\*4: Backdriving torque is the torque value applied to the output side at which the input first starts to rotate. The values in the table are maximum values.

Note: Never rely on these values as a margin in a system that must hold an external load. A brake must be used where back driving is not permissible.

Table 078-3

Load	No load
Speed reducer surface temperature	25°C

\*5: No-load running torque is the torque required at the input to operate the gearhead at a given speed under a no-load condition. The values in the table are average values.

Table 078-4

Input speed	2000 rpm
Load	No load
Speed reducer surface temperature	25°C

## Torsional Stiffness CSF-GH

Table 079-1

Size		14	20	32	45	65
Symbol						
$T_1$	Nm	2.0	7.0	29	76	235
	kgfm	0.2	0.7	3.0	7.8	24
$T_2$	Nm	6.9	25	108	275	843
	kgfm	0.7	2.5	11	28	86
Reduction ratio 50	$K_1$	$\times 10^4 \text{ Nm/rad}$	0.34	1.3	5.4	15
		kgfm/arc min	0.1	0.38	1.6	4.3
	$K_2$	$\times 10^4 \text{ Nm/rad}$	0.47	1.8	7.8	20
		kgfm/arc min	0.14	0.52	2.3	6.0
	$K_3$	$\times 10^4 \text{ Nm/rad}$	0.57	2.3	9.8	26
		kgfm/arc min	0.17	0.67	2.9	7.6
	$\theta_1$	$\times 10^{-4} \text{ rad}$	5.8	5.2	5.5	5.2
		arc min	2.0	1.8	1.9	1.8
	$\theta_2$	$\times 10^{-4} \text{ rad}$	16	15.4	15.7	15.1
		arc min	5.6	5.3	5.4	5.2
Reduction ratio 80 or more	$K_1$	$\times 10^4 \text{ Nm/rad}$	0.47	1.6	6.7	18
		kgfm/arc min	0.14	0.47	2.0	5.4
	$K_2$	$\times 10^4 \text{ Nm/rad}$	0.61	2.5	11	29
		kgfm/arc min	0.18	0.75	3.2	8.5
	$K_3$	$\times 10^4 \text{ Nm/rad}$	0.71	2.9	12	33
		kgfm/arc min	0.21	0.85	3.7	9.7
	$\theta_1$	$\times 10^{-4} \text{ rad}$	4.1	4.4	4.4	4.1
		arc min	1.4	1.5	1.5	1.4
	$\theta_2$	$\times 10^{-4} \text{ rad}$	12	11.3	11.6	11.1
		arc min	4.2	3.9	4.0	3.8

\* The values in this table are average values. See page 88 for more information about torsional stiffness.

## Hysteresis Loss CSF-GH

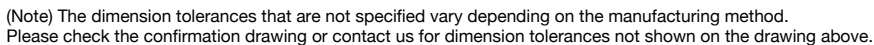
Reduction ratio 50: Approx.  $5.8 \times 10^{-4}$  rad (2arc min)

Reduction ratio 80 or more: Approx.  $2.9 \times 10^{-4}$  rad (1arc min)

Only primary dimensions are shown in the drawings below. Refer to the confirmation drawing for detailed dimensions.

Figure 080-1

(Unit: mm)



(Unit: mm)

Table 080-1

Flange	Coupling	A (H7)		B	C		F (H7)		G		H <sup>+</sup>	Moment of Inertia	Mass (kg) <sup>+</sup>	
		Min.	Max.	Max.	Min.	Max.	Min.	Max.	Min.	Max.	Typical	(10 <sup>-6</sup> kgm <sup>2</sup> )	Shaft	Flange
Type I	1	50	58	7	58	72	6.0	7.8	21.5	32.5	76	0.07	0.88	0.76
Type II	1	30	45	6.5	36	54	6.0	7.8	21.5	32.5	76	0.07	0.90	0.78

\*3 Tapped hole for motor mounting screw.

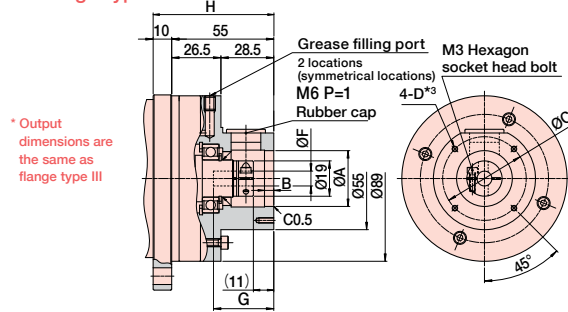
## CSF-GH-20 Outline Dimensions

Only primary dimensions are shown in the drawings below. Refer to the confirmation drawing for detailed dimensions.

Figure 081-1

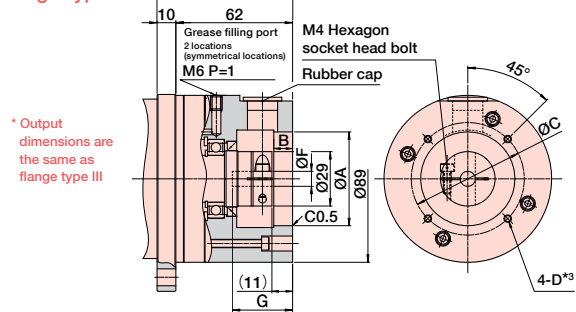
(Unit: mm)

Flange Type I



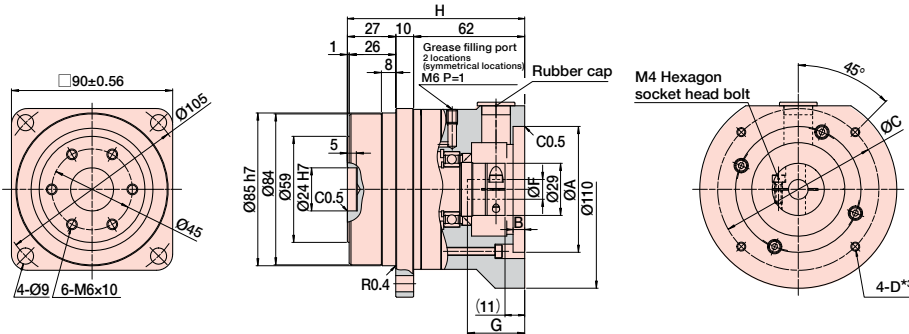
\* Output dimensions are the same as flange type III

Flange Type II

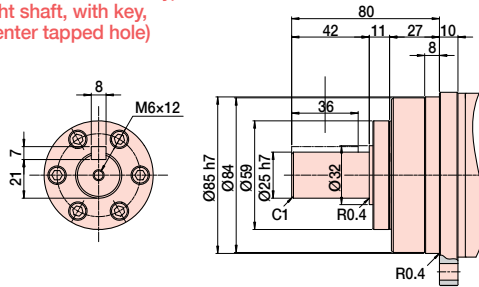


\* Output dimensions are the same as flange type III

Flange Type III



Output shaft shape: J2 (Straight shaft, without key)  
J6 (Straight shaft, with key, with center tapped hole)



(Note) The dimension tolerances that are not specified vary depending on the manufacturing method.  
Please check the confirmation drawing or contact us for dimension tolerances not shown on the drawing above.

## Dimension Table

(Unit: mm)

Table 081-1

Flange	Coupling	A (H7)		B	C		F (H7)		G		H *	Moment of Inertia (10 <sup>-4</sup> kgm <sup>2</sup> )	Mass (kg) **	
		Min.	Max.	Max.	Min.	Max.	Min.	Max.	Min.	Max.	Typical		Shaft	Flange
Type I	1	30	45	5	36	48	7.0	7.8	23.0	33.0	82.0	0.28	2.3	1.9
Type II	2	50	70	10	60	80	8.0	14.6	25.0	32.0	99.0	0.42	2.6	2.2
Type III	2	50	80	10	60	100	8.0	14.6	25.0	32.0	99.0	0.42	2.8	2.4

Refer to the confirmation drawing for detailed dimensions.

Dimensions of typical products are shown. Please contact us for other mounting options if the configurations shown above are not suitable for your particular motor.

\*1 May vary depending on motor interface dimensions.

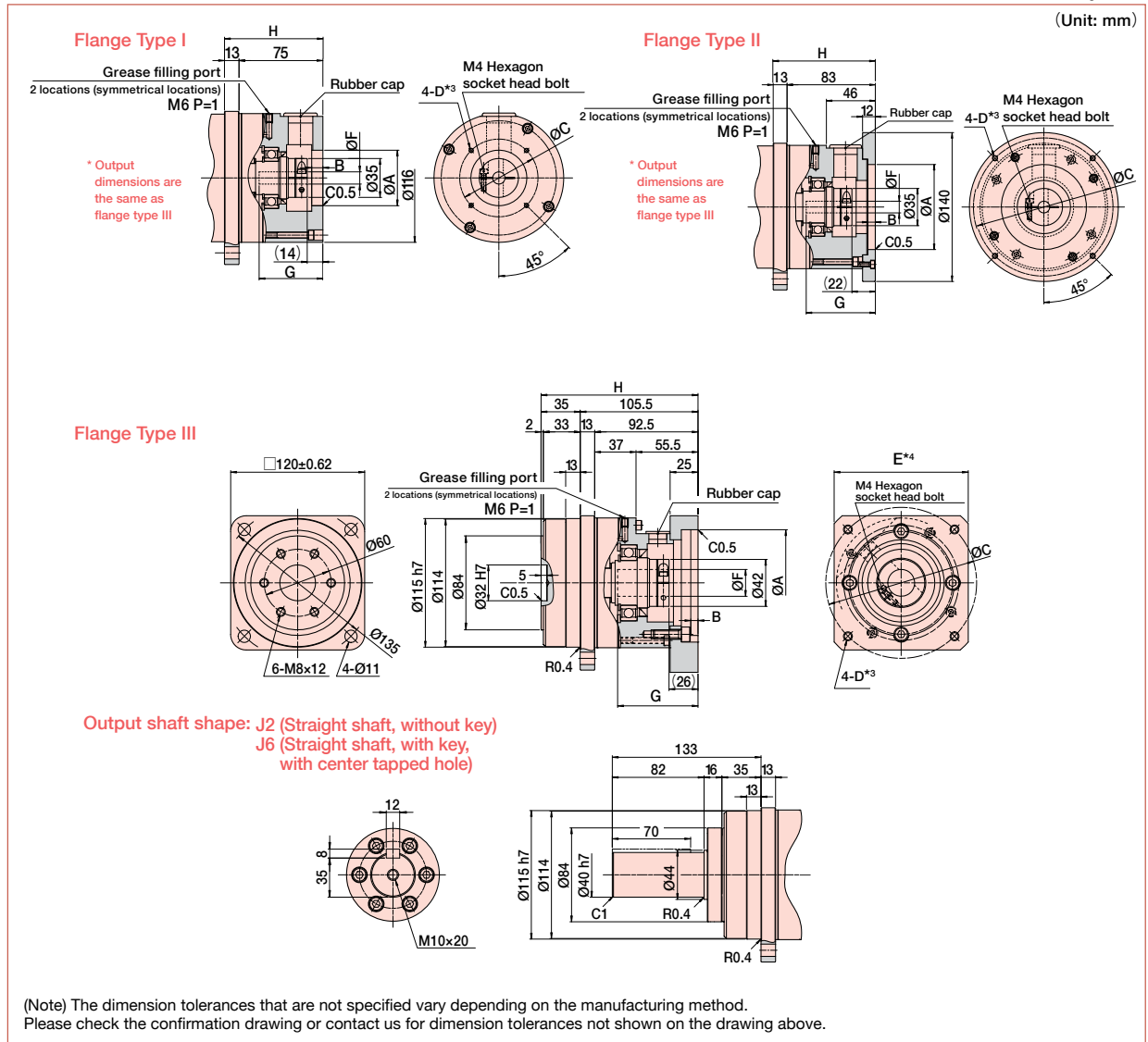
\*2 The mass will vary slightly depending on the ratio and on the inside diameter of the input shaft coupling.

\*3 Tapped hole for motor mounting screw.

## CSF-GH-32 Outline Dimensions

Only primary dimensions are shown in the drawings below. Refer to the confirmation drawing for detailed dimensions.

Figure 082-1



## Dimension Table

(Unit: mm)

Table 082-1

Flange	Coupling	A (H7)		B	C		F (H7)		G		H	Moment of Inertia (10 <sup>-4</sup> kgm <sup>2</sup> )	Mass (kg) **	
		Min.	Max.		Min.	Max.	Min.	Max.	Min.	Max.			Shaft	Flange
Type I	3	50	85	10	58	105	11.0	19.6	28.0	57	133	2.7	6.4	5.0
Type II	2	70	95	5	85	115	16.0	25.8	35.0	67	145.5	2.7	6.6	5.2
Type III	1	95	130	7	115	165	11.0	19.6	36.0	65	141	2.0	7.9	6.5

Refer to the confirmation drawing for detailed dimensions.

Dimensions of typical products are shown. Please contact us for other mounting options if the configurations shown above are not suitable for your particular motor.

\*1 May vary depending on motor interface dimensions.

\*2 The mass will vary slightly depending on the ratio and on the inside diameter of the input shaft coupling.

\*3 Tapped hole for motor mounting screw.

\*4 E dimension is dependent on motor selection.



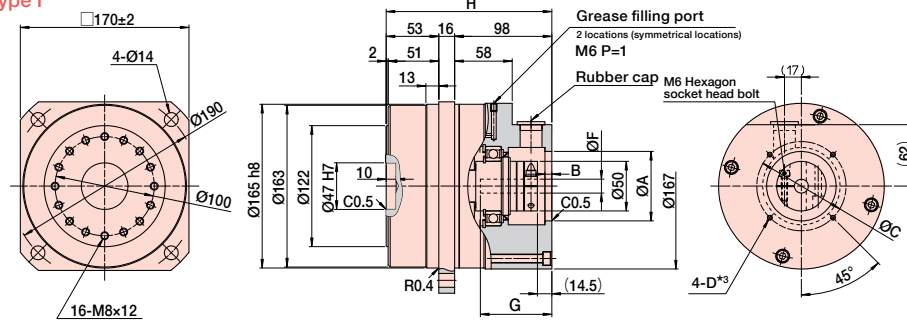
# CSF-GH-45 Outline Dimensions

Only primary dimensions are shown in the drawings below. Refer to the confirmation drawing for detailed dimensions.

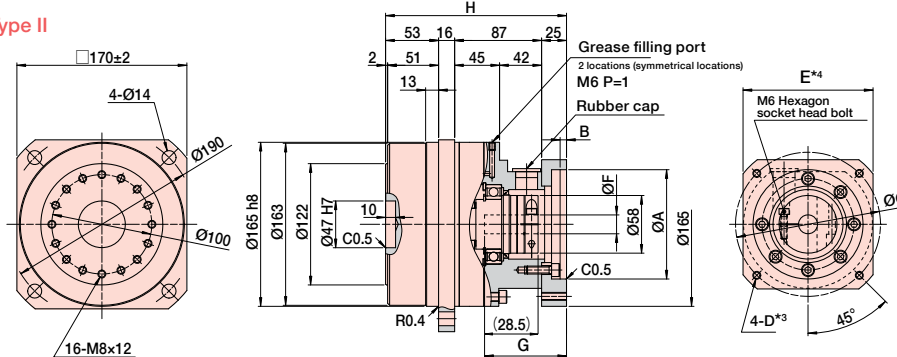
Figure 083-1

(Unit: mm)

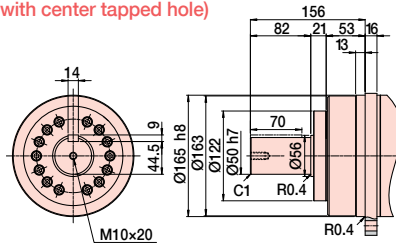
## Flange Type I



## Flange Type II



Output shaft shape: J2 (Straight shaft, without key)  
J6 (Straight shaft, with key, with center tapped hole)



(Note) The dimension tolerances that are not specified vary depending on the manufacturing method.  
Please check the confirmation drawing or contact us for dimension tolerances not shown on the drawing above.

## Dimension Table

(Unit: mm)

Table 083-1

Flange	Coupling	A (H7)		B	C		F (H7)		G		H *	Moment of Inertia (10 <sup>-4</sup> kgm <sup>2</sup> )	Mass (kg) *2	
		Min.	Max.	Max.	Min.	Max.	Min.	Max.	Min.	Max.	Typical		Shaft	Flange
Type I	1	70	110	7	80	150	14.0	29.4	31.5	72	167	11	17.3	14.3
Type I	2	70	110	7	80	150	19.0	41	40.5	77	167	11	17.3	14.3
Type II	1	110	130	6.5	145	200	14.0	29.4	31.5	72	176	11	16.7	13.7
Type II	2	110	130	6.5	145	200	19.0	41	40.5	77	176	11	17.7	14.7

Refer to the confirmation drawing for detailed dimensions.

Dimensions of typical products are shown. Please contact us for other mounting options if the configurations shown above are not suitable for your particular motor.

\*1 May vary depending on motor interface dimensions.

\*2 The mass will vary slightly depending on the ratio and on the inside diameter of the input shaft coupling.

\*3 Tapped hole for motor mounting screw.

\*4 E dimension is dependent on motor selection.



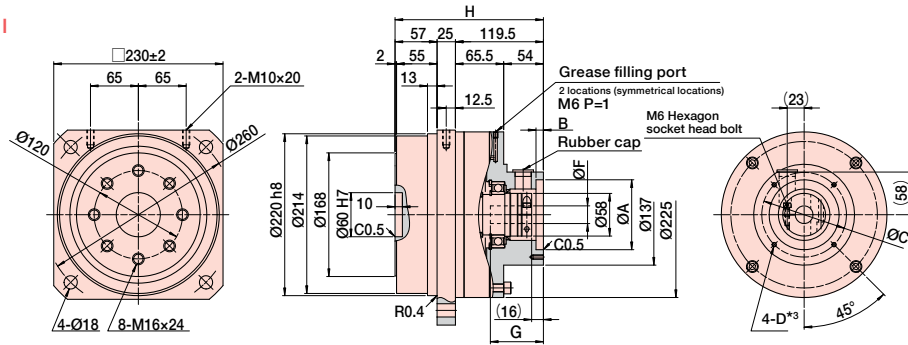
# CSF-GH-65 Outline Dimensions

Only primary dimensions are shown in the drawings below. Refer to the confirmation drawing for detailed dimensions.

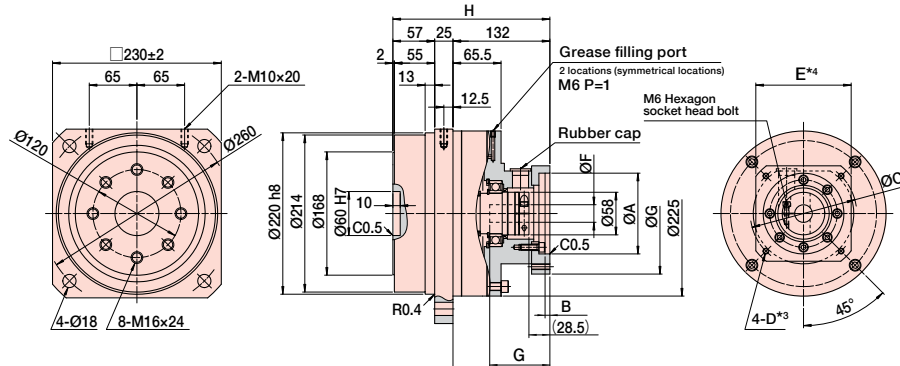
Figure 084-1

(Unit: mm)

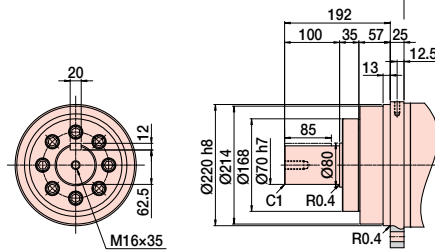
Flange Type I



Flange Type II



Output shaft shape: J2 (Straight shaft, without key)  
J6 (Straight shaft, with key, with center tapped hole)



(Note) The dimension tolerances that are not specified vary depending on the manufacturing method. Please check the confirmation drawing or contact us for dimension tolerances not shown on the drawing above.

## Dimension Table

(Unit: mm)

Table 084-1

Flange	Coupling	A (H7)		B	C		F (H7)		G		H *1	Moment of Inertia (10 <sup>-4</sup> kgm <sup>2</sup> )	Mass (kg) *2	
		Min.	Max.		Min.	Max.	Min.	Max.	Min.	Max.			Shaft	Flange
Type I	1	95	95	10	110	125	19.0	39.3	33.0	72	201.5	51	36.2	27.6
Type II	1	110	200	6.5	145	235	19.0	39.3	40.5	79.5	209	51	38.3	29.7

Refer to the confirmation drawing for detailed dimensions.

Dimensions of typical products are shown. Please contact us for other mounting options if the configurations shown above are not suitable for your particular motor.

\*1 May vary depending on motor interface dimensions.

\*2 The mass will vary slightly depending on the ratio and on the inside diameter of the input shaft coupling.

\*3 Tapped hole for motor mounting screw.

\*4 E dimension is dependent on motor selection.



## Rating Table Definitions

See the corresponding pages of each series for values from the ratings.

### ■ Rated torque

Rated torque indicates allowable continuous load torque at input speed.

### ■ Limit for Repeated Peak Torque (see Graph 086-1)

During acceleration and deceleration the Harmonic Drive® gear experiences a peak torque as a result of the moment of inertia of the output load. The table indicates the limit for repeated peak torque.

### ■ Limit for Average Torque

In cases where load torque and input speed vary, it is necessary to calculate an average value of load torque. The table indicates the limit for average torque. The average torque calculated must not exceed this limit. (calculation formula: Page 91)

### ■ Limit for Momentary Torque (see Graph 086-1)

The gear may be subjected to momentary peak torques in the event of a collision or emergency stop. The magnitude and frequency of occurrence of such peak torques must be kept to a minimum and they should, under no circumstance, occur during normal operating cycle. The allowable number of occurrences of the momentary peak torque may be calculated by using formula 073-1.

### ■ Maximum Average Input Speed Maximum Input Speed

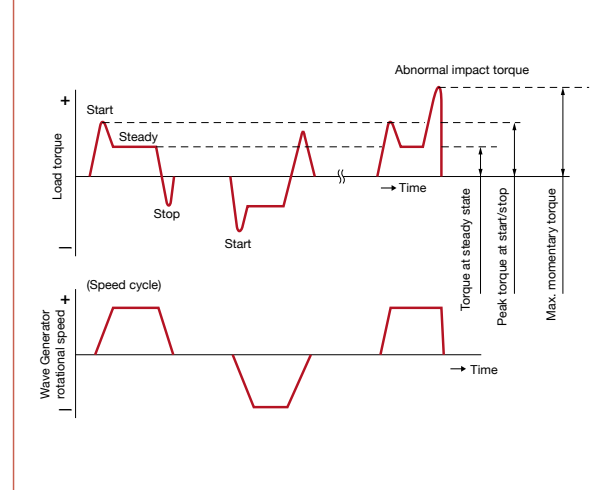
Do not exceed the allowable rating. (calculation formula of the average input speed: Page 91).

### ■ Inertia

The rating indicates the moment of inertia reflected to the gear input.

Example of load torque pattern

Graph 086-1



## Life

### ■ Life of the wave generator

The life of a gear is determined by the life of the wave generator bearing. The life may be calculated by using the input speed and the output load torque.

Table 086-1

Series name	Life	
	CSF-GH	CSG-GH
L <sub>10</sub>	7,000 hours	10,000 hours
L <sub>50</sub> (average life)	35,000 hours	50,000 hours

\* Life is based on the input speed and output load torque from the ratings.

### Calculation formula for Rated Lifetime

Formula 086-1

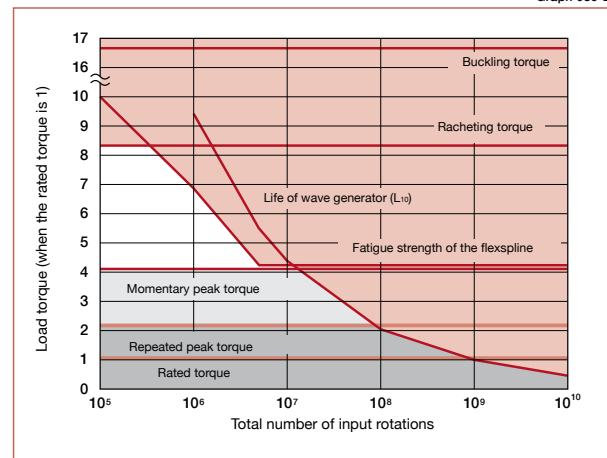
$$L_h = L_n \cdot \left( \frac{T_r}{T_{av}} \right)^3 \cdot \left( \frac{N_r}{N_{av}} \right)$$

Table 086-2

L <sub>n</sub>	Life of L <sub>10</sub> or L <sub>50</sub> C
T <sub>r</sub>	Rated torque
N <sub>r</sub>	Rated input speed
T <sub>av</sub>	Average load torque on the output side (calculation formula: Page 91)
N <sub>av</sub>	Average input speed (calculation formula: Page 91)

Relative torque rating

Graph 086-2



\* Lubricant life not taken into consideration in the graph described above.

\* Use the graph above as reference values.

## Torque Limits

### Strength of flexspline

The Flexspline is subjected to repeated deflections, and its strength determines the torque capacity of the Harmonic Drive® gear. The values given for Rated Torque at Rated Speed and for the allowable Repeated Peak Torque are based on an infinite fatigue life for the Flexspline.

The torque that occurs during a collision must be below the momentary peak torque (impact torque). The maximum number of occurrences is given by the equation below.

Allowable limit of the bending cycles of the flexspline during rotation of the wave generator while the impact torque is applied:  $1.0 \times 10^4$  (cycles)

The torque that occurs during a collision must be below the momentary peak torque (impact torque). The maximum number of occurrences is given by the equation below.

#### Calculation formula

Formula 087-1

$$N = \frac{1.0 \times 10^4}{2 \times \frac{n}{60} \times t}$$

Permissible occurrences	N occurrences
Time that impact torque is applied	t sec
Rotational speed of the wave generator	n rpm
The flexspline bends two times per one revolution of the wave generator.	



If the number of occurrences is exceeded, the Flexspline may experience a fatigue failure.

### Buckling torque

When a highly excessive torque (16 to 17 times rated torque) is applied to the output with the input stationary, the flexspline may experience plastic deformation. This is defined as buckling torque.

\* See the corresponding pages of each series for buckling torque values.



When the flexspline buckles, early failure of the HarmonicDrive® gear may occur.

### Ratcheting torque

When excessive torque (8 to 9 times rated torque) is applied while the gear is in motion, the teeth between the Circular Spline and Flexspline may not engage properly.

This phenomenon is called ratcheting and the torque at which this occurs is called ratcheting torque. Ratcheting may cause the Flexspline to become non-concentric with the Circular Spline. Operating in this condition may result in shortened life and a Flexspline fatigue failure.

\* See the corresponding pages of each series for ratcheting torque values.

\* Ratcheting torque is affected by the stiffness of the housing to be used when installing the circular spline. Contact us for details of the ratcheting torque.

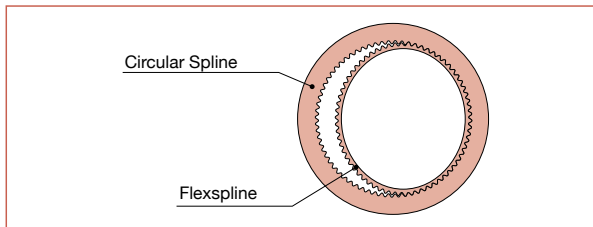


When ratcheting occurs, the teeth may not be correctly engaged and become out of alignment as shown in Figure 087-1. Operating the drive in this condition will cause vibration and damage the flexspline.



Once ratcheting occurs, the teeth wear excessively and the ratcheting torque may be lowered.

Figure 087-1



"Dedoidal" condition.

## Torsional Stiffness

Stiffness and backlash of the drive system greatly affects the performance of the servo system. Please perform a detailed review of these items before designing your equipment and selecting a model number.

### ■ Stiffness

Fixing the input side (wave generator) and applying torque to the output side (flexspline) generates torsion almost proportional to the torque on the output side. Figure 088-1 shows the torsional angle at the output side when the torque applied on the output side starts from zero, increases up to  $+T_0$  and decreases down to  $-T_0$ . This is called the "Torque – torsion angle diagram," which normally draws a loop of  $0 - A - B - A' - B' - A$ . The slope described in the "Torque – torsion angle diagram" is represented as the spring constant for the stiffness of the HarmonicDrive® gear (unit: Nm/rad).

As shown in Figure 074-2, this "Torque – torsional angle diagram" is divided into 3 regions, and the spring constants in the area are represented by  $K_1$ ,  $K_2$  and  $K_3$ .

- $K_1$  .... The spring constant when the torque changes from [zero] to  $[T_1]$
- $K_2$  .... The spring constant when the torque changes from  $[T_1]$  to  $[T_2]$
- $K_3$  .... The spring constant when the torque changes from  $[T_2]$  to  $[T_3]$

- See the corresponding pages of each series for values of the spring constants ( $K_1$ ,  $K_2$ ,  $K_3$ ) and the torque-torsional angles ( $T_1$ ,  $T_2$ ,  $- \theta_1$ ,  $\theta_2$ ).

### ■ Example for calculating the torsion angle

The torsion angle ( $\theta$ ) is calculated here using CSG-32-100-GH as an example.

$$\begin{aligned} T_1 &= 29 \text{ Nm} \\ T_2 &= 108 \text{ Nm} \\ K_1 &= 6.7 \times 10^4 \text{ Nm/rad} \\ K_2 &= 6.7 \times 10^4 \text{ Nm/rad} \\ K_3 &= 6.7 \times 10^4 \text{ Nm/rad} \\ \theta_1 &= 4.4 \times 10^{-4} \text{ rad} \\ \theta_2 &= 11.6 \times 10^{-4} \text{ rad} \end{aligned}$$

**When the applied torque is  $T_1$  or less, the torsion angle  $\theta_{L1}$  is calculated as follows:**

$$\begin{aligned} \text{When the load torque } T_{L1} &= 6.0 \text{ Nm} \\ \theta_{L1} &= T_{L1}/K_1 \\ &= 6.0/6.7 \times 10^4 \\ &= 9.0 \times 10^{-5} \text{ rad (0.31 arc min)} \end{aligned}$$

**When the applied torque is between  $T_1$  and  $T_2$ , the torsion angle  $\theta_{L2}$  is calculated as follows:**

$$\begin{aligned} \text{When the load torque is } T_{L2} &= 50 \text{ Nm} \\ \theta_{L2} &= \theta_1 + (T_{L2} - T_1)/K_2 \\ &= 4.4 \times 10^{-4} + (50 - 29)/11.0 \times 10^4 \\ &= 4.4 \times 10^{-4} + 40.0 \times 10^{-5} \\ &= 8.4 \times 10^{-4} \text{ rad (2.89 arc min)} \end{aligned}$$

**When the applied torque is greater than  $T_2$ , the torsion angle  $\theta_{L3}$  is calculated as follows:**

$$\begin{aligned} \text{When the load torque is } T_{L3} &= 178 \text{ Nm} \\ \theta_{L3} &= \theta_1 + \theta_2 + (T_{L3} - T_2)/K_3 \\ &= 4.4 \times 10^{-4} + 11.6 \times 10^{-4} + (178 - 108)/12.0 \times 10^4 \\ &= 4.4 \times 10^{-4} + 11.6 \times 10^{-4} + 5.8 \times 10^{-4} \\ &= 2.18 \times 10^{-3} \text{ rad (7.5 arc min)} \end{aligned}$$

When a bidirectional load is applied, the total torsion angle will be  $2 \times \theta_{Lx}$  plus hysteresis loss.

\* The torsion angle calculation is for the gear component set only and does not include any torsional windup of the output shaft.

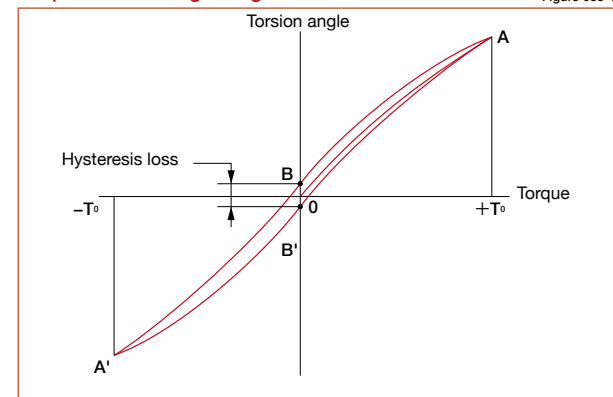
### ■ Hysteresis loss

As shown in Figure 088-1, when the applied torque is increased to the rated torque and is brought back to [zero], the torsional angle does not return exactly back to the zero point. This small difference ( $B - B'$ ) is called hysteresis loss.

- See the appropriate page for each model series for the hysteresis loss value.

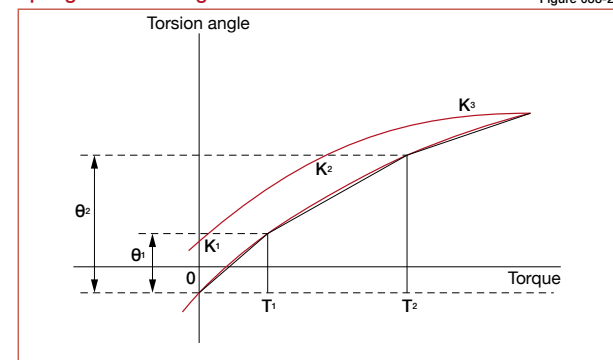
Torque - torsion angle diagram

Figure 088-1



Spring constant diagram

Figure 088-2



### ■ Backlash

Hysteresis loss is primarily caused by internal friction. It is a very small value and will vary roughly in proportion to the applied load. Because HarmonicDrive® gearheads have zero backlash, the only true backlash is due to the clearance in the Oldham coupling, a self-aligning mechanism used on the wave generator. Since the Oldham coupling is used on the input, the backlash measured at the output is extremely small (arc-seconds) since it is divided by the gear reduction ratio.

## Vibration

The primary frequency of the transmission error of the HarmonicDrive® gear may rarely cause a vibration of the load inertia. This can occur when the driving frequency of the servo system including the HarmonicDrive® gear is at, or close to the resonant frequency of the system. Refer to the design guide of each series.

The primary component of the transmission error occurs twice per input revolution of the input. Therefore, the frequency generated by the transmission error is 2x the input frequency (rev / sec).

If the resonant frequency of the entire system, including the HarmonicDrive® gear, is  $F=15$  Hz, then the input speed (N) which would generate that frequency could be calculated with the formula below.

Formula 089-1

$$N = \frac{15}{2} \cdot 60 = 450 \text{ rpm}$$

The resonant frequency is generated at an input speed of 450 rpm.

### How to calculate resonant frequency of the system

Formula 089-2

$$f = \frac{1}{2\pi} \sqrt{\frac{K}{J}}$$

### Formula variables

Table 089-1

f	The resonant frequency of the system	Hz	
K	Spring constant of the HarmonicDrive® gear	Nm/rad	See pages of each series.
J	Load inertia	kgm <sup>2</sup>	

## Efficiency

The efficiency will vary depending on the following factors:

- Reduction ratio
- Input speed
- Load torque
- Temperature
- Lubrication condition (Type of lubricant and the quantity)

## Product Sizing & Selection

In general, a servo system rarely operates at a continuous load and speed. The input rotational speed, load torque change and comparatively large torque are applied at start and stop. Unexpected impact torque may be applied.

These fluctuating load torques should be converted to the average load torque when selecting a model number.

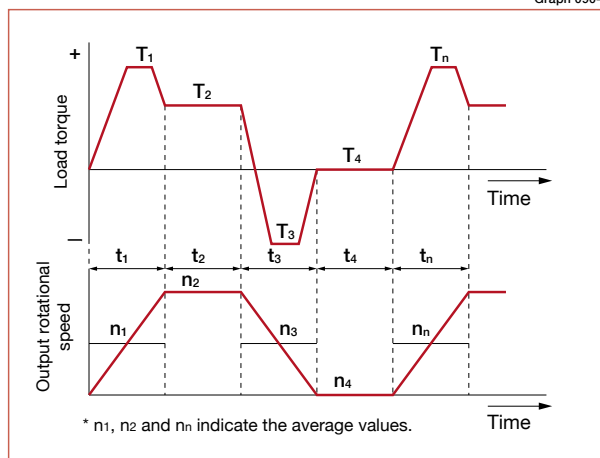
As an accurate cross roller bearing is built in the direct external load support (output flange), the maximum moment load, life of the cross roller bearing and the static safety coefficient should also be checked.

(Note) If HarmonicDrive® CSG-GH series is installed with the output shaft facing downward (motor faces upward) and continuously operated in one direction under the constant load state, lubrication failure may occur. In this case, please contact us for details.

### Checking the load torque pattern

Review the load torque pattern. Check the specifications shown in the figure below.

Graph 090-1



#### Obtain the value of each load torque pattern.

Load torque	$T_n$ (Nm)
Time	$t_n$ (sec)
Output rotational speed	$n_n$ (rpm)

#### <Normal operation pattern>

Starting	$T_1, t_1, n_1$
Steady operation	$T_2, t_2, n_2$
Stopping (slowing)	$T_3, t_3, n_3$
Idle	$T_4, t_4, n_4$

#### <Maximum rotational speed>

Max. output speed	$no_{max}$
Max. input rotational speed	$ni_{max}$
(Restricted by motors)	

#### <Impact torque>

When impact torque is applied	$T_s, t_s, n_s$
-------------------------------	-----------------

#### <Required life>

$$L_{10} = L \text{ (hours)}$$

### Flowchart for selecting a size

Please use the flowchart shown below for selecting a size. Operating conditions must not exceed the performance ratings.

Calculate the average load torque applied on the output side from the load torque pattern:  $T_{av}$  (Nm).

$$T_{av} = \sqrt[3]{\frac{n_1 \cdot t_1 \cdot |T_1|^3 + n_2 \cdot t_2 \cdot |T_2|^3 + \dots + n_n \cdot t_n \cdot |T_n|^3}{n_1 \cdot t_1 + n_2 \cdot t_2 + \dots + n_n \cdot t_n}}$$

Make a preliminary model selection with the following conditions.

$T_{av} \leq \text{Limit for average torque torque}$   
(See the ratings of each series).

Calculate the average output speed:  $no_{av}$  (rpm)

$$no_{av} = \frac{n_1 \cdot t_1 + n_2 \cdot t_2 + \dots + n_n \cdot t_n}{t_1 + t_2 + \dots + t_n}$$

Obtain the reduction ratio (R).  
A limit is placed on "ni max" by motors.

$$\frac{ni_{max}}{no_{max}} \geq R$$

Calculate the average input rotational speed from the average output rotational speed ( $no_{av}$ ) and the reduction ratio (R):  $ni_{av}$  (rpm)

$$ni_{av} = no_{av} \cdot R$$

Calculate the maximum input rotational speed from the max. output rotational speed ( $no_{max}$ ) and the reduction ratio (R):  $ni_{max}$  (rpm)

$$ni_{max} = no_{max} \cdot R$$

Check whether the preliminary model number satisfies the following condition from the ratings.

$$ni_{av} \leq \text{Limit for average speed (rpm)}$$

$$ni_{max} \leq \text{Limit for maximum speed (rpm)}$$

OK

Check whether  $T_1$  and  $T_3$  are equal to or less than the repeated peak torque specification.

OK

Check whether  $T_s$  is equal to or less than the the momentary peak torque specification.

OK

Calculate ( $N_s$ ) the allowable number of rotations during impact torque.

$$N_s = \frac{10^4}{2 \cdot \frac{n_s \cdot R}{60} \cdot t} \dots \dots N_s \leq 1.0 \times 10^4$$

OK

Calculate the lifetime.

$$L_{10} = 7000 \cdot \left( \frac{T_r}{T_{av}} \right)^3 \cdot \left( \frac{nr}{ni_{av}} \right) \text{ (hours)}$$

Check whether the calculated lifetime is equal to or more than the life of the wave generator (see Page 086).

OK

The model number is confirmed.

Review the operation conditions and model number



## Example of model number selection

### Value of each load torque pattern.

Load torque	$T_n$ (Nm)
Time	$t_n$ (sec)
Output speed	$n_n$ (rpm)

### <Normal operation pattern>

Starting	$T_1 = 400$ Nm, $t_1 = 0.3$ sec, $n_1 = 7$ rpm
Steady operation	$T_2 = 320$ Nm, $t_2 = 3$ sec, $n_2 = 14$ rpm
Stopping (slowing)	$T_3 = 200$ Nm, $t_3 = 0.4$ sec, $n_3 = 7$ rpm
Idle	$T_4 = 0$ Nm, $t_4 = 0.2$ sec, $n_4 = 0$ rpm

### <Maximum rotational speed>

Max. output speed	no $max = 14$ rpm
Max. input speed (Restricted by motors)	ni $max = 1800$ rpm

### <Impact torque>

When impact torque is applied	$T_s = 500$ Nm, $t_s = 0.15$ sec, $n_s = 14$ rpm
-------------------------------	---

### <Required life>

$L_{10} = 7000$  (hours)

Calculate the average load torque applied on the output side of the Harmonic Drive® gear from the load torque pattern:  $T_{av}$  (Nm).

$$T_{av} = \sqrt[3]{\frac{7 \text{ rpm} \cdot 0.3 \text{ sec} \cdot |400 \text{ Nm}|^3 + 14 \text{ rpm} \cdot 3 \text{ sec} \cdot |320 \text{ Nm}|^3 + 7 \text{ rpm} \cdot 0.4 \text{ sec} \cdot |200 \text{ Nm}|^3}{7 \text{ rpm} \cdot 0.3 \text{ sec} + 14 \text{ rpm} \cdot 3 \text{ sec} + 7 \text{ rpm} \cdot 0.4 \text{ sec}}}$$

Make a preliminary model selection with the following conditions.  $T_{av} = 319$  Nm  $\leq 620$  Nm  
(Limit for average torque for model number CSF-45-120-GH: See the ratings on Page 77.)

Thus, **CSF-45-120-GH** is tentatively selected.

Calculate the average output rotational speed: no  $av$  (rpm)

$$\text{no } av = \frac{7 \text{ rpm} \cdot 0.3 \text{ sec} + 14 \text{ rpm} \cdot 3 \text{ sec} + 7 \text{ rpm} \cdot 0.4 \text{ sec}}{0.3 \text{ sec} + 3 \text{ sec} + 0.4 \text{ sec} + 0.2 \text{ sec}} = 12 \text{ rpm}$$

Obtain the reduction ratio (R).

$$\frac{1800 \text{ rpm}}{14 \text{ rpm}} = 128.6 \geq 120$$

Calculate the average input rotational speed from the average output rotational speed (no  $av$ ) and the reduction ratio (R): ni  $av$  (rpm)

$$\text{ni } av = 12 \text{ rpm} \cdot 120 = 1440 \text{ rpm}$$

Calculate the maximum input rotational speed from the maximum output rotational speed (no  $max$ ) and the reduction ratio (R): ni  $max$  (rpm)

$$\text{ni } max = 14 \text{ rpm} \cdot 120 = 1680 \text{ rpm}$$

Check whether the preliminary selected model number satisfies the following condition from the ratings.

ni  $av = 1440$  rpm  $\leq 3000$  rpm (Max average input speed of size 45)  
ni  $max = 1680$  rpm  $\leq 3800$  rpm (Max input speed of size 45)

NG

OK

Check whether  $T_1$  and  $T_3$  are equal to or less than the repeated peak torque specification.

$T_1 = 400$  Nm  $\leq 823$  Nm (Limit of repeated peak torque of size 45)  
 $T_3 = 200$  Nm  $\leq 823$  Nm (Limit of repeated peak torque of size 45)

NG

OK

Check whether  $T_s$  is equal to or less than the momentary peak torque specification.

$T_s = 500$  Nm  $\leq 1760$  Nm (Limit for momentary torque of size 45)

NG

OK

Calculate the allowable number ( $N_s$ ) rotation during impact torque and confirm  $\leq 1.0 \times 10^4$

$$N_s = \frac{10^4}{2 \cdot \frac{14 \text{ rpm} \cdot 120}{60} \cdot 0.15 \text{ sec}} = 1190 \leq 1.0 \times 10^4$$

NG

OK

Calculate the lifetime.

$$L_{10} = 7000 \cdot \left( \frac{402 \text{ Nm}}{319 \text{ Nm}} \right)^3 \cdot \left( \frac{2000 \text{ rpm}}{1440 \text{ rpm}} \right) \text{ (hours)}$$

Check whether the calculated life is equal to or more than the life of the wave generator (see Page 86).

$L_{10} = 19,457$  hours  $\geq 7000$  (life of the wave generator:  $L_{10}$ )

NG

OK

The selection of model number **CSF-45-120-GH** is confirmed from the above calculations.

Review the operation conditions and model number

# HarmonicDrive® CSG/CSF-GH Series

HarmonicDrive® gearing has a unique operating principle which utilizes the elastic mechanics of metals. This precision gear reducer consists of only 3 basic parts and provides high accuracy and repeatability.



#### Wave Generator

The Wave Generator is a thin raced ball bearing fitted onto an elliptical shaped hub. The inner race of the bearing is fixed to the cam and the outer race is elastically deformed into an ellipse via the balls. The Wave Generator is usually mounted onto the input shaft.

#### Flexspline

The Flexspline is a non-rigid, thin cylindrical cup with external teeth. The Flexspline fits over the Wave Generator and takes on its elliptical shape. The Flexspline is generally used as the output of the gear.

#### Circular Spline

The Circular Spline is a rigid ring with internal teeth, engaging the teeth of the Flexspline across the major axis of the Wave Generator. The Circular Spline has two more teeth than the Flexspline and is generally mounted to the housing.

The greatest benefit of HarmonicDrive® gearing is the weight and space savings compared to other gearheads because it consists of only three basic parts. Since many teeth are engaged simultaneously, it can transmit higher torque and provides high accuracy. A unique S tooth profile significantly improves torque capacity, life and torsional stiffness of the gear.

- ◆ **Zero-backlash**
- ◆ **High Reduction ratios, 50:1 to 160:1 in a single stage**
- ◆ **High precision positioning (repeatability  $\pm 4$  to  $\pm 10$  arc-sec)**
- ◆ **High capacity cross roller output bearing**
- ◆ **High torque capacity**

Robust cross roller bearing is integrated with the output flange to provide high moment stiffness, high load capacity and precise positioning accuracy.

Flexspline

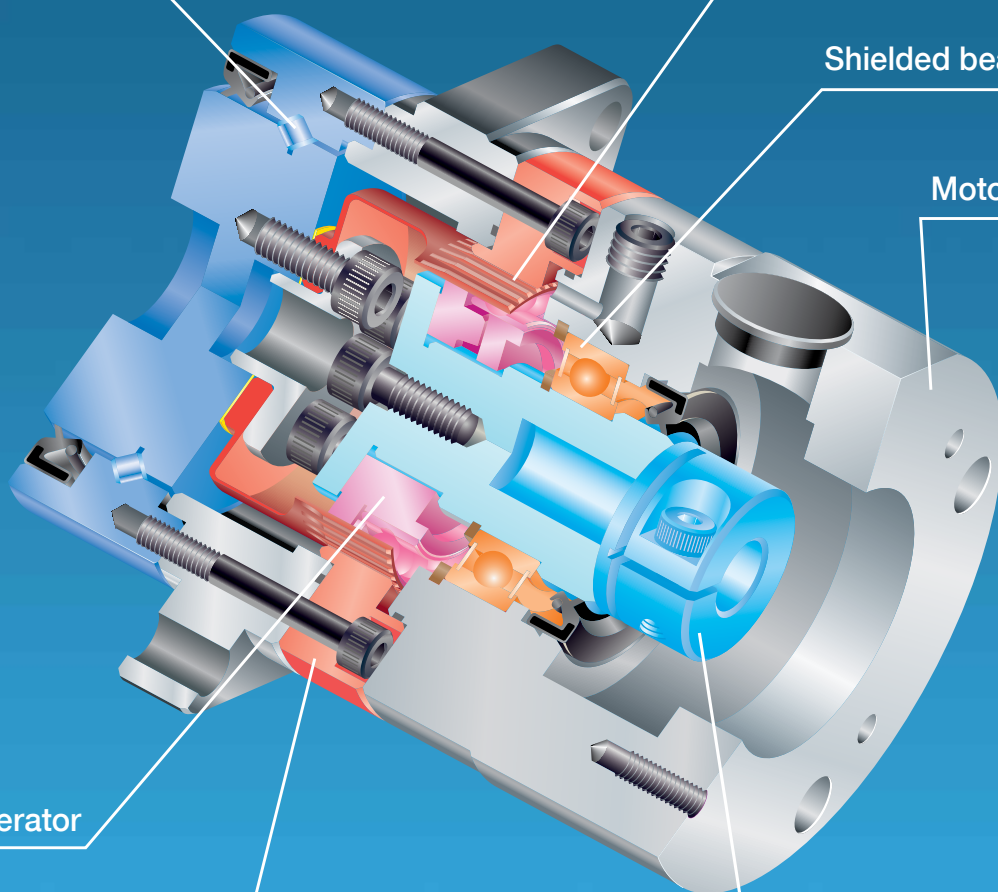
Shielded bearing

Motor mounting flange

Wave Generator

Circular Spline

Quick Connect™ coupling for easy mounting of any servomotor



## Output Bearing Specifications and Checking Procedure

A precision cross roller bearing supports the external load (output flange).  
Check the maximum load, moment load, life of the bearing and static safety coefficient to maximize performance.

### Checking procedure

#### (1) Checking the maximum load moment load ( $M_{max}$ )

Obtain the maximum load moment load ( $M_{max}$ ). ••➡ Maximum load moment load ( $M_{max}$ )  $\leq$  Permissible moment ( $M_c$ )

#### (2) Checking the life

Obtain the average radial load ( $F_{rav}$ ) and the average axial load ( $F_{aav}$ ). ••➡ Obtain the radial load coefficient (X) and the axial load coefficient (Y). ••➡ Calculate the life and check it.

#### (3) Checking the static safety coefficient

Obtain the static equivalent radial load coefficient ( $P_o$ ). ••➡ Check the static safety coefficient. ( $f_s$ )

### Specification of output bearing

#### CSG-GH/CSF-GH Series

Table 130-1 indicates the specifications for cross roller bearing.

Table 130-1

Size	Pitch circle	Offset amount	Basic load rating				Allowable moment load $M_c^{*3}$		Moment stiffness $Km^{*4}$		Allowable radial load <sup>*5</sup>	Allowable axial load <sup>*5</sup>
	dp	R	Basic dynamic load rating $C^{*1}$		Basic static load rating $C_o^{*2}$		Nm	kgfm	$\times 10^4$ Nm/rad	kgfm/ arc min	N	N
	m	m	N	kgf	N	kgf						
14	0.0405	0.011	5110	521	7060	720	27	2.76	3.0	0.89	732	1093
20	0.064	0.0115	10600	1082	17300	1765	145	14.8	17	5.0	1519	2267
32	0.085	0.014	20500	2092	32800	3347	258	26.3	42	12	2938	4385
45	0.123	0.019	41600	4245	76000	7755	797	81.3	100	30	5962	8899
65	0.170	0.0225	81600	8327	149000	15204	2156	220	323	96	11693	17454

\*1 The basic dynamic load rating means a certain static radial load so that the basic dynamic rated life of the roller bearing is a million rotations.

\*2 The basic static load rating means a static load that gives a certain level of contact stress ( $4\text{kN/mm}^2$ ) in the center of the contact area between rolling element receiving the maximum load and orbit.

\*3 The allowable moment load is a maximum moment load applied to the bearing. Within the allowable range, basic performance is maintained and the bearing is operable. Check the bearing life based on the calculations shown on the next page.

\*4 The value of the moment stiffness is the average value.

\*5 The allowable radial load and allowable axial load are the values that satisfy the life of a speed reducer when a pure radial load or an axial load applies to the main bearing. ( $L_r + R = 0$  mm for radial load and  $L_a = 0$  mm for axial load) If a compound load applies, refer to the calculations shown on the next page.

## How to calculate the maximum load moment load

HPGP

HPG

CSG-GH

CSF-GH

HPF

Maximum load moment load ( $M_{max}$ ) is obtained as follows.  
Make sure that  $M_{max} \leq M_c$ .

Formula 131-1

$$M_{max} = Fr_{max}(L_r + R) + Fa_{max} L_a$$

$Fr_{max}$	Max. radial load	N (kgf)	See Fig. 131-1.
$Fa_{max}$	Max. axial load	N (kgf)	See Fig. 131-1.
$L_r, L_a$	—	m	See Fig. 131-1.
$R$	Offset amount	m	See Fig. 131-1. See "Specification of main bearing" of each series

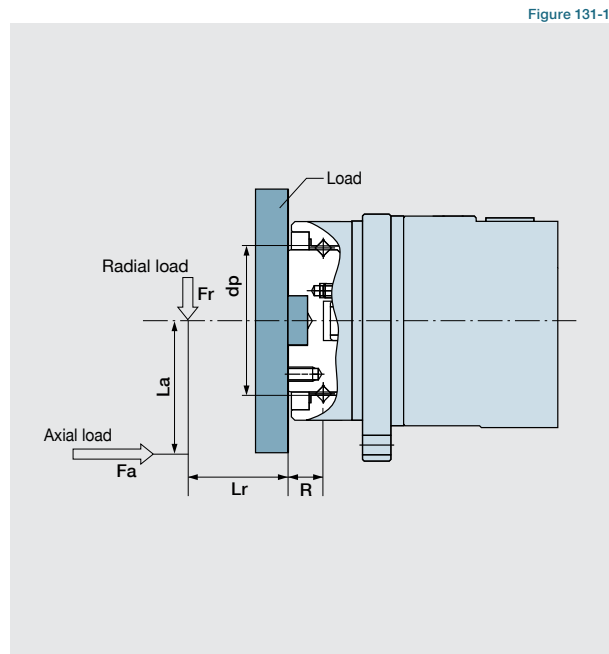


Figure 131-1

## How to calculate the radial load coefficient and the axial load coefficient

HPGP

HPG

CSG-GH

CSF-GH

HPF

The radial load coefficient (X) and the axial load coefficient (Y)

Formula 131-2

Formula	X	Y
$\frac{Fa_{av}}{Fr_{av} + 2(Fr_{av}(L_r + R) + Fa_{av} \cdot L_a) / dp} \leq 1.5$	1	0.45
$\frac{Fa_{av}}{Fr_{av} + 2(Fr_{av}(L_r + R) + Fa_{av} \cdot L_a) / dp} > 1.5$	0.67	0.67

$Fr_{av}$	Average radial load	N (kgf)	See "How to obtain the average load."
$Fa_{av}$	Average axial load	N (kgf)	See "How to obtain the average load."
$L_r, L_a$	—	m	See Fig. 131-1.
$R$	Offset amount	m	See Fig. 131-1. See "Output Shaft Bearing Specifications" of each series.
$dp$	Circular pitch of roller	m	See Fig. 131-1. See "Output Shaft Bearing Specifications" of each series.

## How to calculate the average load (Average radial load, average axial load, average output rotational frequency)

HPGP

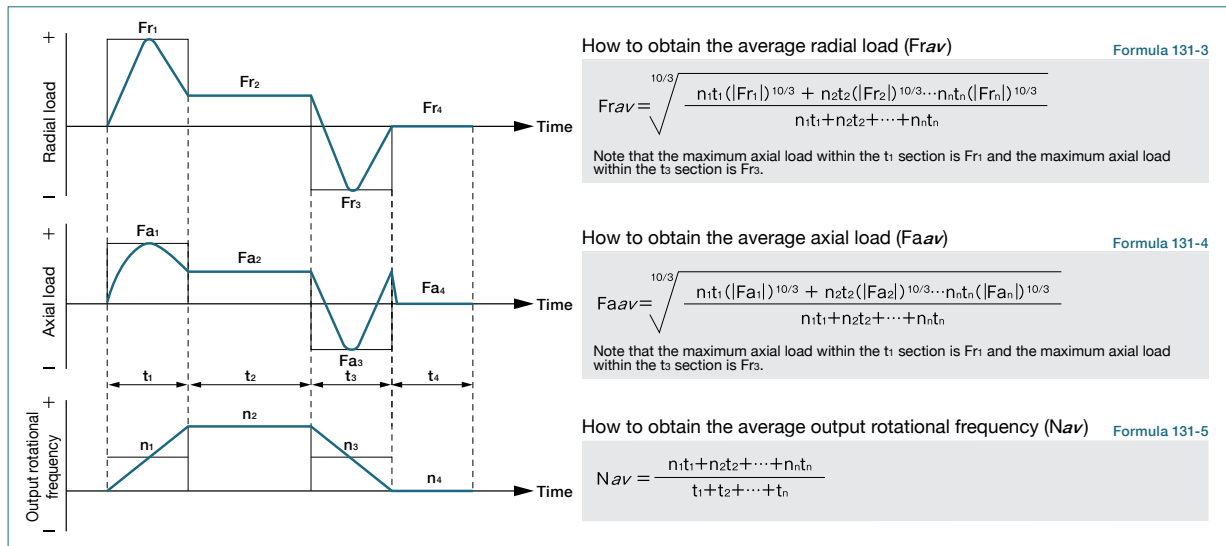
HPG

CSG-GH

CSF-GH

HPF

If the radial load and the axial load fluctuate, they should be converted into the average load to check the life of the cross roller bearing.



## How to calculate the life

HPGP

HPG

CSG-GH

CSF-GH

HPF

Calculate the life of the cross roller bearing using Formula 132-1. You can obtain the dynamic equivalent radial load ( $P_c$ ) using Formula 132-2.

Formula 132-1

$$L_{10} = \frac{10^6}{60 \times N_{av}} \times \left( \frac{C}{f_w \cdot P_c} \right)^{10/3}$$

<b>L<sub>10</sub></b>	Life	hour	—
<b>N<sub>av</sub></b>	Ave. output speed	rpm	See "How to calculate the ave. load."
<b>C</b>	Basic dynamic rated load	N (kgf)	See "Output Bearing Specs."
<b>P<sub>c</sub></b>	Dynamic equi. radial load	N (kgf)	See Formula 132-2.
<b>f<sub>w</sub></b>	Load coefficient	—	See Table 132-1.

Formula 132-2

$$P_c = X \cdot \left( Fr_{av} + \frac{2(Fr_{av}(L_r + R) + Fa_{av} \cdot La)}{dp} \right) + Y \cdot Fa_{av}$$

<b>Fr<sub>av</sub></b>	Average radial load	N (kgf)	See "How to calculate the ave. load."
<b>Fa<sub>av</sub></b>	Average axial load	N (kgf)	See "How to calculate the ave. load."
<b>dp</b>	Circular pitch of roller	m	See "Output Bearing Specs."
<b>X</b>	Radial load coefficient	—	See "How to calculate the radial load coefficient and the axial load coefficient."
<b>Y</b>	Axial load coefficient	—	See "How to calculate the radial load coefficient and the axial load coefficient."
<b>L<sub>r</sub>, La</b>	—	m	See Figure 131-1. See "External load influence diagram."
<b>R</b>	Offset amount	m	See Figure 131-1. See "External load influence diagram" and "Output Bearing Specs" of each series.

## Load coefficient

Table 132-1

Load status	f <sub>w</sub>
During smooth operation without impact or vibration	1 to 1.2
During normal operation	1.2 to 1.5
During operation with impact or vibration	1.5 to 3

## How to calculate the life during oscillating movement

HPGP

HPG

CSG-GH

CSF-GH

HPF

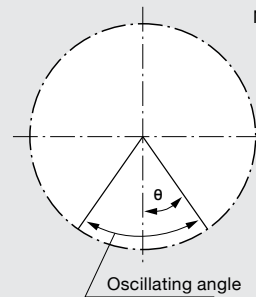
Calculate the life of the cross roller bearing during oscillating movement by Formula 132-3.

Figure 132-1

Formula 132-3

$$Loc = \frac{10^6}{60 \times n_1} \times \frac{90}{\theta} \times \left( \frac{C}{f_w \cdot P_c} \right)^{10/3}$$

<b>Loc</b>	Rated life under oscillating movement	hour	—
<b>n<sub>1</sub></b>	No. of reciprocating oscillation per min.	cpm	—
<b>C</b>	Basic dynamic rated load	N (kgf)	See "Output Bearing Specs."
<b>P<sub>c</sub></b>	Dynamic equivalent radial load	N (kgf)	See Formula 132-2.
<b>f<sub>w</sub></b>	Load coefficient	—	See Table 132-1.
<b>θ</b>	Oscillating angle /2	Deg.	See Figure 132-1.



Note: When the oscillating angle is small (5° or less), it is difficult to generate an oil film on the contact surface of the orbit ring, and the rolling element and fretting may be generated. Contact us if this happens.

## Note

When it is used for a long time while the rotation speed of the output shaft is in the ultra-low operation range (0.02rpm or less), the lubrication of the bearing becomes insufficient, resulting in deterioration of the bearing or increased load in the driving side. When using it in the ultra-low operation range, contact us.

## How to calculate the static safety coefficient

HPGP

HPG

CSG-GH

CSF-GH

HPF

In general, the basic static rated load ( $C_0$ ) is considered to be the permissible limit of the static equivalent load. However, obtain the limit based on the operating and required conditions. Calculate the static safety coefficient ( $f_s$ ) of the cross roller bearing using Formula 132-4.

General values under the operating condition are shown in Table 132-2. You can calculate the static equivalent radial load ( $P_0$ ) using Formula 132-5.

Formula 132-4

$$f_s = \frac{C_0}{P_0}$$

<b>C<sub>0</sub></b>	Basic static rated load	N (kgf)	See "Output Bearing Specs."
<b>P<sub>0</sub></b>	Static equivalent radial load	N (kgf)	See Formula 132-5.

Formula 132-5

$$P_0 = Fr_{max} + \frac{2M_{max}}{dp} + 0.44Fa_{max}$$

<b>Fr<sub>max</sub></b>	Max. radial load	N (kgf)	See "How to calculate the max. load moment load."
<b>Fa<sub>max</sub></b>	Max. axial load	N (kgf)	See "How to calculate the max. load moment load."
<b>M<sub>max</sub></b>	Max. load moment load	Nm (kgfm)	See "How to calculate the max. load moment load."
<b>dp</b>	Circular pitch of roller	m	See "Output Bearing Specs" of each series.

## Static safety coefficient

Table 132-2

Load status	f <sub>s</sub>
When high rotation precision is required	≥ 3
When impact or vibration is expected	≥ 2
Under normal operating condition	≥ 1.5

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